MACHINE LEARNING LAB MANUAL

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1. Scheme and Syllabus:

MACHINE LEARNING LABORATORY

[As per Choice Based Credit System (CBCS) scheme]

(Effective from the academic year 2016 -2017)

SEMESTER – VII

Subject Code	15CSL76	IA Marks	**20**
Number of Lecture Hours/Week	01I + 02P	Exam Marks	**80**
Total Number of Lecture Hours	40	Exam Hours	**3**

CREDITS – 02

Course objectives: This course will enable students to

1. Make use of Data sets in implementing the machine learning algorithms

2. Implement the machine learning concepts and algorithms in any suitable language of

choice.

Description (If any):

1. The programs can be implemented in either JAVA or Python.

2. For Problems 1 to 6 and 10, programs are to be developed without using the built-in

classes or APIs of Java/Python.

3. Data sets can be taken from standard repositories

(https://archive.ics.uci.edu/ml/datasets.html) or constructed by the students.

Lab Experiments:

1   Implement and demonstrate the **FIND-Salgorithm** for finding the most specific hypothesis based on a given set of training data samples. Read the training data from a .CSV file. **(Page NO: 4)**

2   For a given set of training data examples stored in a .CSV file, implement and demonstrate the **Candidate-Elimination algorithm**to output a description of the set of all hypotheses consistent with the training examples. **(Page NO:8)**

3   Write a program to demonstrate the working of the decision tree based **ID3 algorithm**. Use an appropriate data set for building the decision tree and apply this knowledge toclassify a new sample. **(Page NO18:)**

4   Build an Artificial Neural Network by implementing the **Backpropagation algorithm** and test the same using appropriate data sets. **(Page NO:38)**

5   Write a program to implement the **naïve Bayesian classifier** for a sample training data set stored as a .CSV file. Compute the accuracy of the classifier, considering few test data sets. **(Page NO:44)**

6   Assuming a set of documents that need to be classified, use the **naïve Bayesian Classifier** model to perform this task. Built-in Java classes/API can be used to write the program. Calculate the accuracy, precision, and recall for your data set. **(Page NO:52)**

7   Write a program to construct a**Bayesian network** considering medical data. Use this model to demonstrate the diagnosis of heart patients using standard Heart Disease Data Set. You can use Java/Python ML library classes/API. **(Page NO: 61)**

8   Apply **EM algorithm** to cluster a set of data stored in a .CSV file. Use the same data set for clustering using *k*-**Means algorithm**. Compare the results of these two algorithms and comment on the quality of clustering. You can add Java/Python ML library classes/API in the program. **(Page NO: 67)**

9   Write a program to implement *k*-**Nearest Neighbour algorithm** to classify the iris data set. Print both correct and wrong predictions. Java/Python ML library classes can

be used for this problem. **(Page NO: 77)**

10   Implement the non-parametric **Locally Weighted Regressionalgorithm** in order to

fit data points. Select appropriate data set for your experiment and draw graphs. **(Page NO: 82)**

Course outcomes: The students should be able to:

1. Understand the implementation procedures for the machine learning algorithms.

2. Design Java/Python programs for various Learning algorithms.

3. Applyappropriate data sets to the Machine Learning algorithms.

4. Identify and apply Machine Learning algorithms to solve real world problems.

Conduction of Practical Examination:

- All laboratory experiments are to be included for practical examination.

- Students are allowed to pick one experiment from the lot.

- Strictly follow the instructions as printed on the cover page of answer script

- Marks distribution: Procedure + Conduction + Viva:**20 + 50 +10 (80)**

Change of experiment is allowed only once and marks allotted to the procedure part to be made zero.

Problem1 : Implement and demonstrate the **FIND-S algorithm** for finding the most specific hypothesis based on a given set of training data samples. Read the training data from a **.CSV file.**

Algorithm :

1. Initialize **h** to the most specific hypothesis in **H**
2. **For** each positive training instance **x**
   - **For** each attribute constraint a_i in **h**
      If the constraint a_i in **h** is satisfied by **x** then do nothing
         else replace a_i in h by the next more general constraint that is satisfied by **x**
3. Output hypothesis **h**

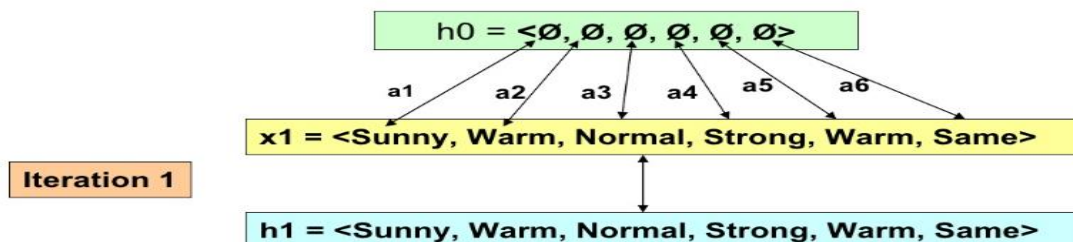## Illustration:

Step1: Find S

Example	Sky	AirTemp	Humidity	Wind	Water	Forecast	EnjoySport
1	Sunny	Warm	Normal	Strong	Warm	Same	Yes
2	Sunny	Warm	High	Strong	Warm	Same	Yes
3	Rainy	Cold	High	Strong	Warm	Change	No
4	Sunny	Warm	High	Strong	Cool	Change	Yes

1. Initialize h to the most specific hypothesis in H

h0 = <Ø, Ø, Ø, Ø, Ø, Ø>

Step2 : Find S

2. For each positive training instance x
   - For each attribute constraint a_i in h
      If the constraint a_i is satisfied by x
      Then do nothing
      Else replace a_i in h by the next more general constraint that is satisfied by x

h0 = <Ø, Ø, Ø, Ø, Ø, Ø>

a1   a2   a3   a4   a5   a6

x1 = <Sunny, Warm, Normal, Strong, Warm, Same>

Iteration 1

h1 = <Sunny, Warm, Normal, Strong, Warm, Same>

Step2 : Find S

Iteration 2

h1 = <Sunny, Warm, Normal, Strong, Warm, Same>

x2 = <Sunny, Warm, High, Strong, Warm, Same>

h2 = <Sunny, Warm, ?, Strong, Warm, Same>

Iteration 3   Ignore   h3 = <Sunny, Warm, ?, Strong, Warm, Same>
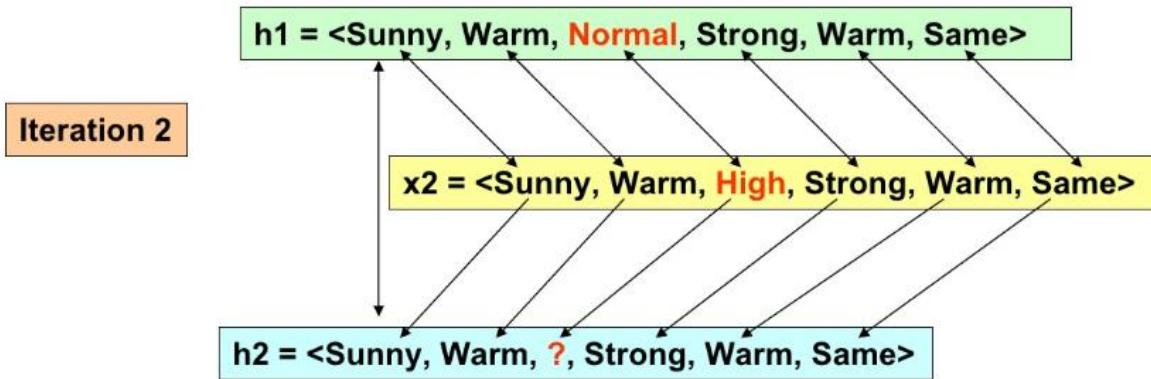
Iteration 4 and Step 3 : Find S

Iteration 4

h3 = < Sunny, Warm, ?, Strong, Warm, Same >

x4 = < Sunny, Warm, High, Strong, Cool, Change >

Step 3

Output   h4 = <Sunny, Warm, ?, Strong, ?, ?>
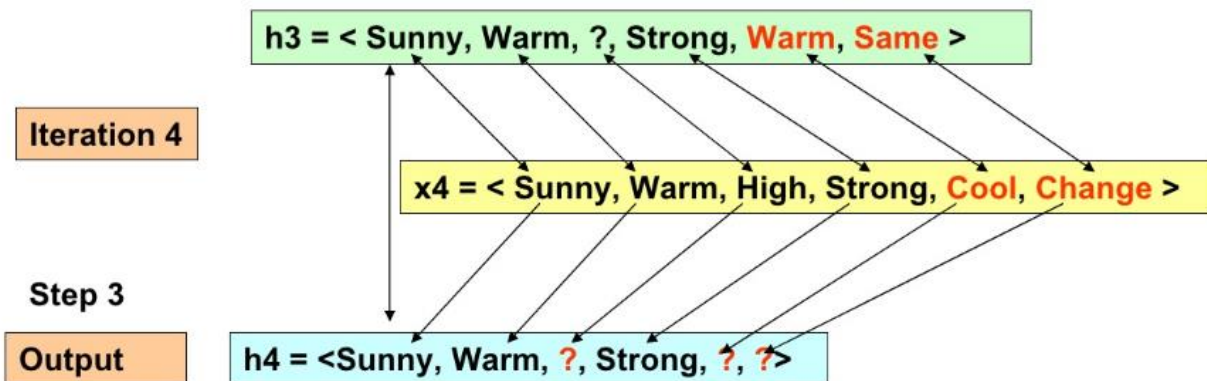
Source Code of the Program :

```python
import random
import csv


attributes = [['Sunny','Rainy'],
              ['Warm','Cold'],
              ['Normal','High'],
              ['Strong','Weak'],
              ['Warm','Cool'],
              ['Same','Change']]


num_attributes = len(attributes)


print (" \n The most general hypothesis : ['?','?','?','?','?','?']\n")
print ("\n The most specific hypothesis : ['0','0','0','0','0','0']\n")

a = []
print("\n The Given Training Data Set \n")

with open('C:\\Users\\thyagaragu\\Desktop\\Data\\ws.csv', 'r') as csvFile:
    reader = csv.reader(csvFile)
    for row in reader:
        a.append (row)
        print(row)


print("\n The initial value of hypothesis: ")
hypothesis = ['0'] * num_attributes
print(hypothesis)

# Comparing with First Training Example
for j in range(0,num_attributes):
        hypothesis[j] = a[0][j];

# Comparing with Remaining Training Examples of Given Data Set

print("\n Find S: Finding a Maximally Specific Hypothesis\n")

for i in range(0,len(a)):
    if a[i][num_attributes]=='Yes':
```

```python
            for j in range(0,num_attributes):
                if a[i][j]!=hypothesis[j]:
                    hypothesis[j]='?'
                else :
                    hypothesis[j]= a[i][j]
    print(" For Training Example No :{0} the hypothesis is ".format(i),hypothesis)

print("\n The Maximally Specific Hypothesis for a given Training Examples :\n")
print(hypothesis)
```

Output :

The most general hypothesis : ['?','?','?','?','?','?']
The most specific hypothesis : ['0','0','0','0','0','0']
The Given Training Data Set
['sunny', 'warm', 'normal', 'strong', 'warm', 'same', 'Yes']
['sunny', 'warm', 'high', 'strong', 'warm', 'same', 'Yes']
['rainy', 'cold', 'high', 'strong', 'warm', 'change', 'No']
['sunny', 'warm', 'high', 'strong', 'cool', 'change', 'Yes']
The initial value of hypothesis:
['0', '0', '0', '0', '0', '0']
Find S: Finding a Maximally Specific Hypothesis
For Training Example No :0 the hypothesis is ['sunny', 'warm', 'normal', 'strong', 'warm', 'same']
For Training Example No :1 the hypothesis is ['sunny', 'warm', '?', 'strong', 'warm', 'same']
For Training Example No :2 the hypothesis is ['sunny', 'warm', '?', 'strong', 'warm', 'same']
For Training Example No :3 the hypothesis is ['sunny', 'warm', '?', 'strong', '?', '?']
The Maximally Specific Hypothesis for a given Training Examples :
['sunny', 'warm', '?', 'strong', '?', '?']

Program2 : For a given set of training data examples stored in a .CSV file, implement and demonstrate the Candidate - elimination algorithm to output a description of the set of all hypotheses consistent with the training examples.

Algorithm:

$G \leftarrow$ **maximally general hypotheses in H**
$S \leftarrow$ **maximally specific hypotheses in H**
For each training example d=<x,c(x)>
Case 1 : If d is a positive example
 Remove from G any hypothesis that is inconsistent with d
 For each hypothesis s in S that is not consistent with d
  • *Remove s from S.*
  • *Add to S all minimal generalizations h of s such that*
   • *h consistent with d*
   • *Some member of G is more general than h*
  • *Remove from S any hypothesis that is more general than another hypothesis in S*
Case 2: If d is a negative example
 Remove from S any hypothesis that is inconsistent with d
 For each hypothesis g in G that is not consistent with d
  • *Remove g from G.*
  • *Add to G all minimal specializations h of g such that*
   ○ *h consistent with d*
   ○ *Some member of S is more specific than h*
  • *Remove from G any hypothesis that is less general than another hypothesis in G*

Illustration :

Example	Sky	AirTemp	Humidity	Wind	Water	Forecast	EnjoySport
1	Sunny	Warm	Normal	Strong	Warm	Same	Yes
2	Sunny	Warm	High	Strong	Warm	Same	Yes
3	Rainy	Cold	High	Strong	Warm	Change	No
4	Sunny	Warm	High	Strong	Cool	Change	Yes

$S_0 = \{<\varnothing, \varnothing, \varnothing, \varnothing, \varnothing, \varnothing>\}$
$G_0 = \{<?, ?, ?, ?, ?, ?>\}$

$S_1 = \{<Sunny, Warm, Normal, Strong, Warm, Same>\}$
$G_1 = \{<?, ?, ?, ?, ?, ?>\}$

$S_2 = \{<Sunny, Warm, ?, Strong, Warm, Same>\}$
$G_2 = \{<?, ?, ?, ?, ?, ?>\}$
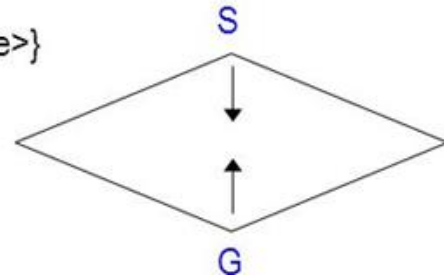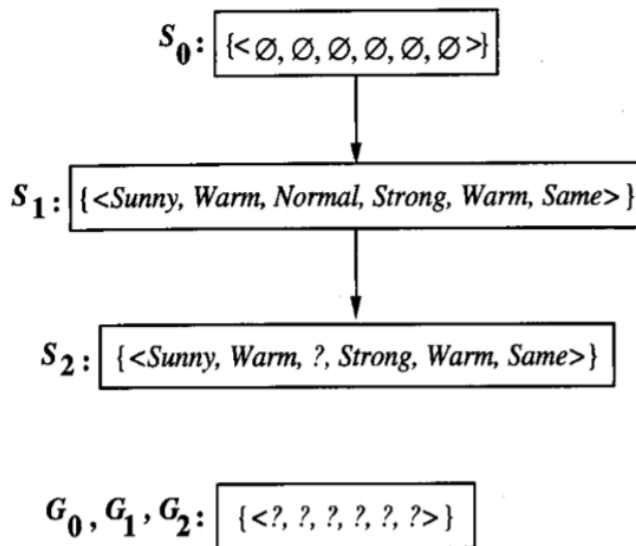
Trace1 :

Training examples:

1. *<Sunny, Warm, Normal, Strong, Warm, Same>, Enjoy Sport = Yes*

2. *<Sunny, Warm, High, Strong, Warm, Same>, Enjoy Sport = Yes*

CANDIDATE-ELIMINATION Trace 1. S_0 and G_0 are the initial boundary sets corresponding to the most specific and most general hypotheses. Training examples 1 and 2 force the S boundary to become more general, as in the FIND-S algorithm. They have no effect on the G boundary.

Trace 2:

S_2, S_3: { <Sunny, Warm, ?, Strong, Warm, Same> }

G_3: {<Sunny, ?, ?, ?, ?, ?>   <?, Warm, ?, ?, ?, ?>   <?, ?, ?, ?, ?, Same>}

G_2: {<?, ?, ?, ?, ?, ?> }
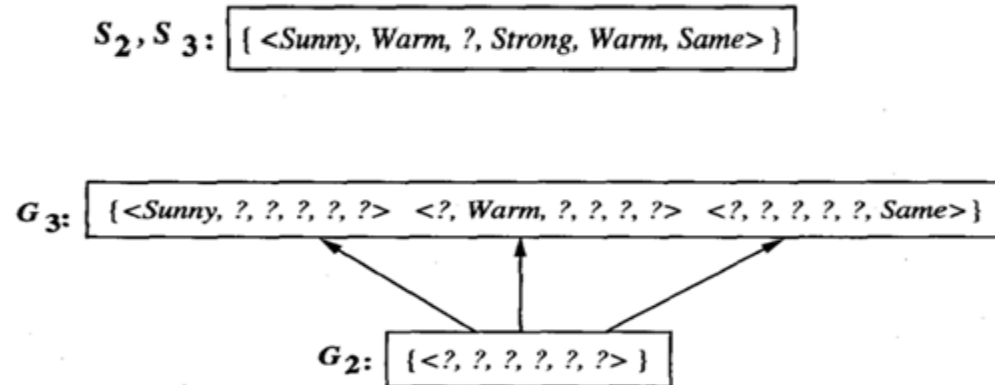
Training Example:

3. <Rainy, Cold, High, Strong, Warm, Change>, EnjoySport=No

CANDIDATE-ELIMINATION Trace 2. Training example 3 is a negative example that forces the G_2 boundary to be specialized to G_3. Note several alternative maximally general hypotheses are included in G_3.

Trace3 :

S_3: {<Sunny, Warm, ?, Strong, Warm, Same>}

S_4: { <Sunny, Warm, ?, Strong, ?, ?> }

G_4: {<Sunny, ?, ?, ?, ?, ?>   <?, Warm, ?, ?, ?, ?>}

G_3: {<Sunny, ?, ?, ?, ?, ?>   <?, Warm, ?, ?, ?, ?>   <?, ?, ?, ?, ?, Same>}
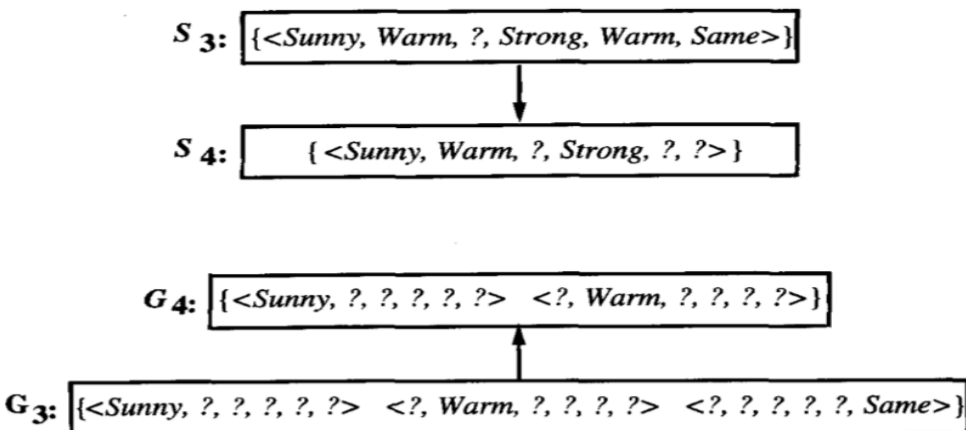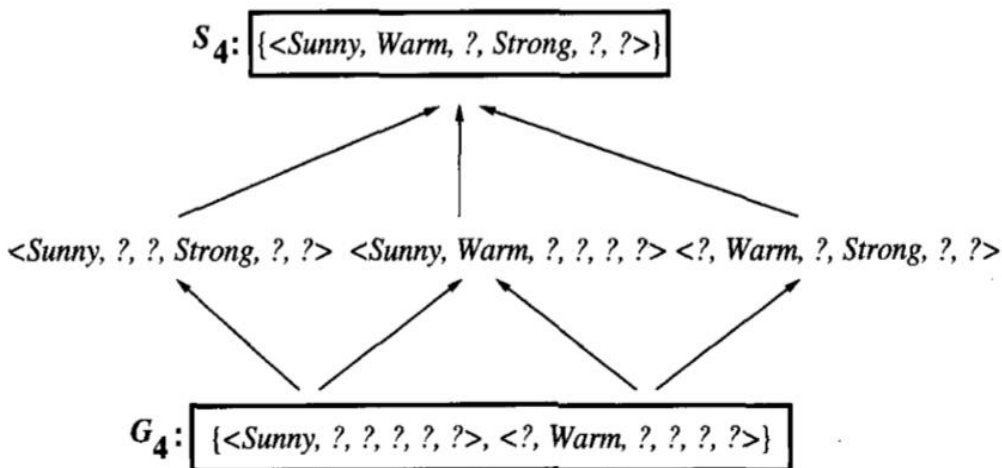
Training Example:

4. <Sunny, Warm, High, Strong, Cool, Change>, EnjoySport = Yes

CANDIDATE-ELIMINATION Trace 3. The positive training example generalizes the S boundary, from S_3 to S_4. One member of G_3 must also be deleted, because it is no longer more general than the S_4 boundary.

Final Version Space:

The final version space for the *EnjoySport* concept learning problem and training examples described earlier.

Source Code :

```python
# Author : Dr.Thyagaraju G S , Context Innovations Lab , DEpt of CSE , SDM
IT - Ujire
# Date : July 11 2018
# Refrence : https://www.uni-weimar.de/fileadmin/user/fak/medien/professur
en/Webis/teaching/
# ws15/machine-learning/concept-learning.slides.html#/4
import random
import csv

def g_0(n):
    return ("?",)*n

def s_0(n):
    return ('0',)*n


def more_general(h1, h2):
    more_general_parts = []
    for x, y in zip(h1, h2):
        mg = x == "?" or (x != "0" and (x == y or y == "0"))
        more_general_parts.append(mg)
    return all(more_general_parts)

l1 = [1, 2, 3]
l2 = [3, 4, 5]
```

```python
list(zip(l1, l2))
[(1, 3), (2, 4), (3, 5)]
```

```python
# min_generalizations
def fulfills(example, hypothesis):
    ### the implementation is the same as for hypotheses:
    return more_general(hypothesis, example)

def min_generalizations(h, x):
    h_new = list(h)
    for i in range(len(h)):
        if not fulfills(x[i:i+1], h[i:i+1]):
            h_new[i] = '?' if h[i] != '0' else x[i]
    return [tuple(h_new)]

min_generalizations(h=('0', '0'  , 'sunny'),
                    x=('rainy', 'windy', 'cloudy'))
[('rainy', 'windy', '?')]
```

```python
def min_specializations(h, domains, x):
    results = []
    for i in range(len(h)):
        if h[i] == "?":
            for val in domains[i]:
                if x[i] != val:
                    h_new = h[:i] + (val,) + h[i+1:]
                    results.append(h_new)
        elif h[i] != "0":
            h_new = h[:i] + ('0',) + h[i+1:]
            results.append(h_new)
    return results
```

```python
min_specializations(h=('?', 'x',),
                    domains=[['a', 'b', 'c'], ['x', 'y']],
                    x=('b', 'x'))
```

```python
[('a', 'x'), ('c', 'x'), ('?', '0')]
```

```python
with open('C:\\Users\\thyagaragu\\Desktop\\Data\\c1.csv')  as csvFile:
        examples = [tuple(line) for line in csv.reader(csvFile)]

#examples = [('sunny', 'warm', 'normal', 'strong', 'warm', 'same',True),
# ('sunny', 'warm', 'high', 'strong', 'warm', 'same',True),
# ('rainy', 'cold', 'high', 'strong', 'warm', 'change',False),
# ('sunny', 'warm', 'high', 'strong', 'cool', 'change',True)]
```

```
examples
[('Sunny', 'Warm', 'Normal', 'Strong', 'Warm', 'Same', 'Y'),
 ('Sunny', 'Warm', 'High', 'Strong', 'Warm', 'Same', 'Y'),
 ('Rainy', 'Cold', 'High', 'Strong', 'Warm', 'Change', 'N'),
 ('Sunny', 'Warm', 'High', 'Strong', 'Cool', 'Change', 'Y')]
def get_domains(examples):
    d = [set() for i in examples[0]]
    for x in examples:
        for i, xi in enumerate(x):
            d[i].add(xi)
    return [list(sorted(x)) for x in d]

get_domains(examples)
```

```
[['Rainy', 'Sunny'],
 ['Cold', 'Warm'],
 ['High', 'Normal'],
 ['Strong'],
 ['Cool', 'Warm'],
 ['Change', 'Same'],
 ['N', 'Y']]
def candidate_elimination(examples):
    domains = get_domains(examples)[:-1]

    G = set([g_0(len(domains))])
    S = set([s_0(len(domains))])
    i=0
    print("\n G[{0}]:".format(i),G)
    print("\n S[{0}]:".format(i),S)
    for xcx in examples:
        i=i+1
        x, cx = xcx[:-1], xcx[-1]  # Splitting data into attributes and decisions
        if cx=='Y': # x is positive example
            G = {g for g in G if fulfills(x, g)}
            S = generalize_S(x, G, S)
        else: # x is negative example
            S = {s for s in S if not fulfills(x, s)}
            G = specialize_G(x, domains, G, S)
        print("\n G[{0}]:".format(i),G)
        print("\n S[{0}]:".format(i),S)
    return
```

```python
def generalize_S(x, G, S):
    S_prev = list(S)
    for s in S_prev:
        if s not in S:
            continue
        if not fulfills(x, s):
            S.remove(s)
            Splus = min_generalizations(s, x)
            ## keep only generalizations that have a counterpart in G
            S.update([h for h in Splus if any([more_general(g,h)
                                        for g in G])])
            ## remove hypotheses less specific than any other in S
            S.difference_update([h for h in S if
                                any([more_general(h, h1)
                                    for h1 in S if h != h1])])
    return S
```

```python
def specialize_G(x, domains, G, S):
    G_prev = list(G)
    for g in G_prev:
        if g not in G:
            continue
        if fulfills(x, g):
            G.remove(g)
            Gminus = min_specializations(g, domains, x)
            ## keep only specializations that have a conuterpart in S
            G.update([h for h in Gminus if any([more_general(h, s)
                                        for s in S])])
            ## remove hypotheses less general than any other in G
            G.difference_update([h for h in G if
                                any([more_general(g1, h)
                                    for g1 in G if h != g1])])
    return G
```

```python
candidate_elimination(examples)
```

output :

```
G[0]: {('?', '?', '?', '?', '?', '?')}

 S[0]: {('0', '0', '0', '0', '0', '0')}

 G[1]: {('?', '?', '?', '?', '?', '?')}

 S[1]: {('Sunny', 'Warm', 'Normal', 'Strong', 'Warm', 'Same')}
```

```
G[2]: {('?', '?', '?', '?', '?', '?')}

S[2]: {('Sunny', 'Warm', '?', 'Strong', 'Warm', 'Same')}

G[3]: {('Sunny', '?', '?', '?', '?', '?'), ('?', 'Warm', '?', '?', '?', '
?'), ('?', '?', '?', '?', '?', 'Same')}

S[3]: {('Sunny', 'Warm', '?', 'Strong', 'Warm', 'Same')}

G[4]: {('Sunny', '?', '?', '?', '?', '?'), ('?', 'Warm', '?', '?', '?', '
?')}

S[4]: {('Sunny', 'Warm', '?', 'Strong', '?', '?')}
```

Program3: Write a program to demonstrate the working of the decision tree based ID3 algorithm. Use an appropriate data set for building the decision tree and apply this knowledge to classify a new sample.

Algorithm :

ID3 - Algorithm

ID3*(Examples, TargetAttribute, Attributes)*

- Create a *Root* node for the tree
- If all *Examples* are positive, Return the single-node tree *Root*, with label = +
- If all *Examples* are negative, Return the single-node tree *Root*, with label = -
- If *Attributes* is empty, Return the single-node tree Root, with label = most common value of *TargetAttribute* in *Examples*
- Otherwise Begin
  - A ← the attribute from *Attributes* that best classifies *Examples*
  - The decision attribute for *Root* ← A
  - For each possible value, vi, of A,
    - Add a new tree branch below *Root*, corresponding to the test A = vi
    - Let *Examples*$_{vi}$ be the subset of *Examples* that have value vi for A
    - If *Examples*$_{vi}$ is empty
      - Then below this new branch add a leaf node with label = most common value of *TargetAttribute* in *Examples*
      - Else below this new branch add the subtree
        ID3(*Examples*$_{vi}$, *TargetAttribute*, *Attributes* − {A})
- End
- Return *Root*

Illustration:

To illustrate the operation of ID3, let's consider the learning task represented by the below examples

Day	Outlook	Temperature	Humidity	Wind	PlayTennis
D1	Sunny	Hot	High	Weak	No
D2	Sunny	Hot	High	Strong	No
D3	Overcast	Hot	High	Weak	Yes
D4	Rain	Mild	High	Weak	Yes
D5	Rain	Cool	Normal	Weak	Yes
D6	Rain	Cool	Normal	Strong	No
D7	Overcast	Cool	Normal	Strong	Yes
D8	Sunny	Mild	High	Weak	No
D9	Sunny	Cool	Normal	Weak	Yes
D10	Rain	Mild	Normal	Weak	Yes
D11	Sunny	Mild	Normal	Strong	Yes
D12	Overcast	Mild	High	Strong	Yes
D13	Overcast	Hot	Normal	Weak	Yes
D14	Rain	Mild	High	Strong	No

Compute the Gain and identify which attribute is the best as illustrated below

Which attribute is the best classifier?

Gain (S, Humidity)
= .940 - (7/14).985 - (7/14).592
= .151
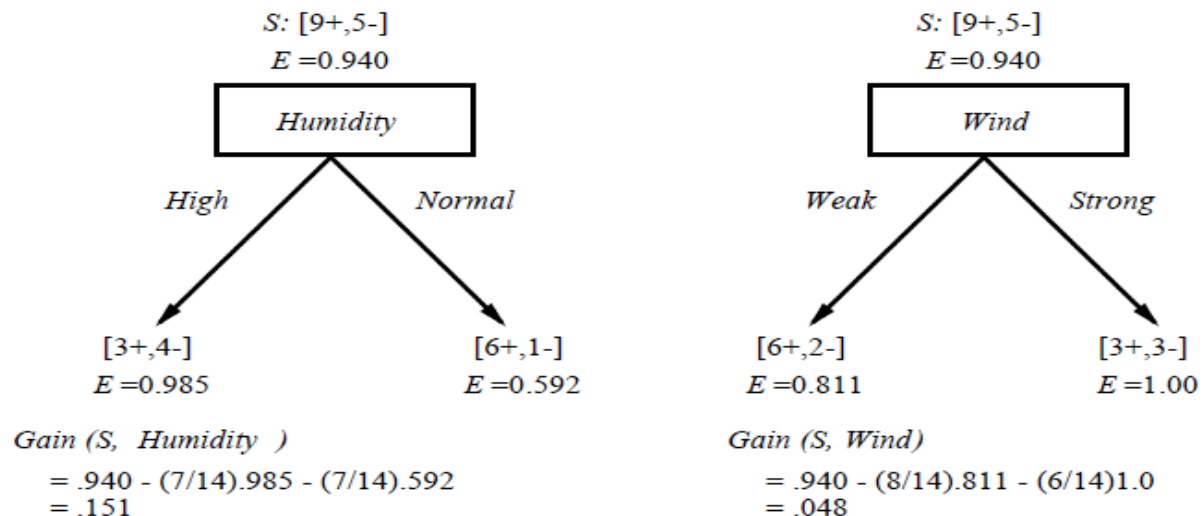
Gain (S, Wind)
= .940 - (8/14).811 - (6/14)1.0
= .048

- Which attribute should be tested at the root?
    - *Gain(S, Outlook)* = 0.246
    - *Gain(S, Humidity)* = 0.151
    - *Gain(S, Wind)* = 0.048
    - *Gain(S, Temperature)* = 0.029
- *Outlook* provides the best prediction for the target
- Lets grow the tree:
    - add to the tree a successor for each possible value of *Outlook*
    - partition the training samples according to the value of *Outlook*

After first step

{D1, D2, ..., D14}

[9+,5−]

Outlook

Sunny   Overcast   Rain

{D1,D2,D8,D9,D11}   {D3,D7,D12,D13}   {D4,D5,D6,D10,D14}

[2+,3−]   [4+,0−]   [3+,2−]

?   Yes   ?
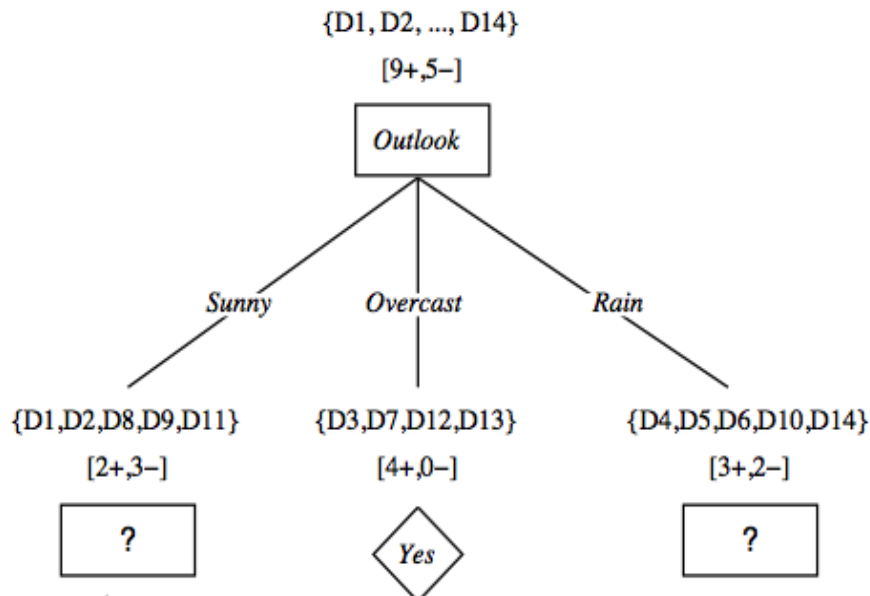
Second step

- Working on *Outlook=Sunny* node:

    $Gain(S_{Sunny}, Humidity)$ = 0.970 − 3/5 × 0.0 − 2/5 × 0.0 = 0.970

    $Gain(S_{Sunny}, Wind)$ = 0.970 − 2/5 × 1.0 − 3.5 × 0.918 = 0.019

    $Gain(S_{Sunny}, Temp.)$ = 0.970 − 2/5 × 0.0 − 2/5 × 1.0 − 1/5 × 0.0 = 0.570
- *Humidity* provides the best prediction for the target
- Lets grow the tree:
    - add to the tree a successor for each possible value of *Humidity*
    - partition the training samples according to the value of *Humidity*

S_{sunny} = {D1,D2,D8,D9,D11}

Gain $(S_{sunny}$, Humidity) = .970 − (3/5) 0.0 − (2/5) 0.0 = .970

Gain $(S_{sunny}$, Temperature) = .970 − (2/5) 0.0 − (2/5) 1.0 − (1/5) 0.0 = .570

Gain $(S_{sunny}$, Wind) = .970 − (2/5) 1.0 − (3/5) .918 = .019

Import Play Tennis Data

```python
import pandas as pd
from pandas import DataFrame
df_tennis = DataFrame.from_csv('C:\\Users\\Dr.Thyagaraju\\Deskto
p\\Data\\PlayTennis.csv')
df_tennis
```

Output :

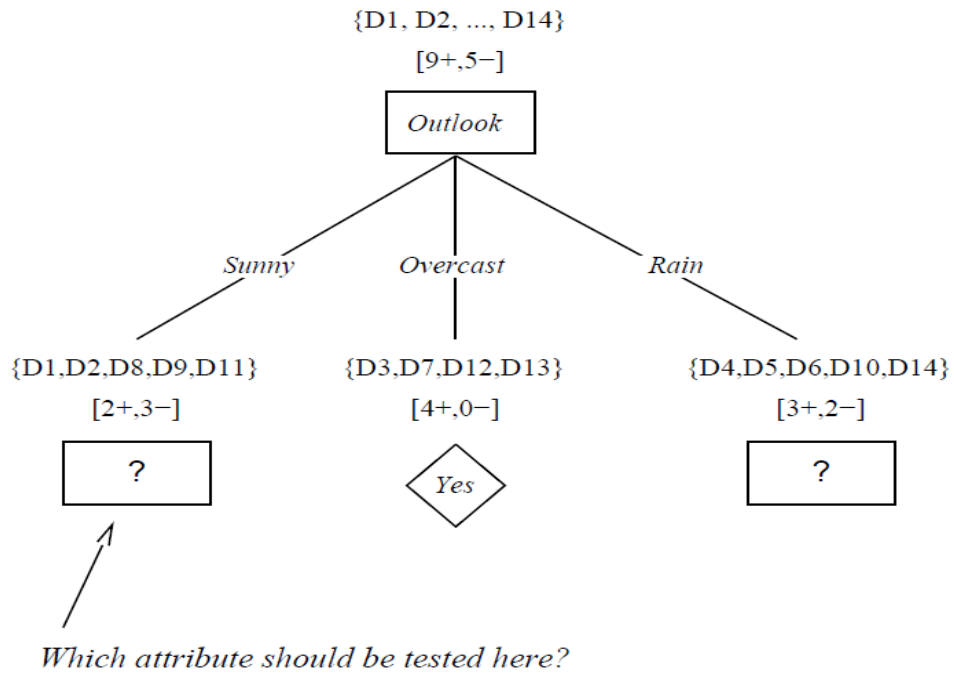|	Play Tennis	Outlook	Temperature	Humidity	Wind
0	No	Sunny	Hot	High	Weak
1	No	Sunny	Hot	High	Strong
2	Yes	Overcast	Hot	High	Weak
3	Yes	Rain	Mild	High	Weak
4	Yes	Rain	Cool	Normal	Weak
5	No	Rain	Cool	Normal	Strong
6	Yes	Overcast	Cool	Normal	Strong
7	No	Sunny	Mild	High	Weak
8	Yes	Sunny	Cool	Normal	Weak
9	Yes	Rain	Mild	Normal	Weak
10	Yes	Sunny	Mild	Normal	Strong
11	Yes	Overcast	Mild	High	Strong
12	Yes	Overcast	Hot	Normal	Weak
13	No	Rain	Mild	High	Strong

Entropy of the Training Data Set

```python
def entropy(probs):   # Calulate the Entropy of given probability
    import math
    return sum( [-prob*math.log(prob, 2) for prob in probs] )

def entropy_of_list(a_list): # Entropy calculation of list of discrete val
ues (YES/NO)
    from collections import Counter
    cnt = Counter(x for x in a_list)
```

```python
    print("No and Yes Classes:",a_list.name,cnt)
    num_instances = len(a_list)*1.0
    probs = [x / num_instances for x in cnt.values()]
    return entropy(probs) # Call Entropy:

# The initial entropy of the YES/NO attribute for our dataset.
#print(df_tennis['PlayTennis'])
total_entropy = entropy_of_list(df_tennis['PlayTennis'])
print("Entropy of given PlayTennis Data Set:",total_entropy)
```

Output :

```
No and Yes Classes: PlayTennis Counter({'Yes': 9, 'No': 5})
Entropy of given PlayTennis Data Set: 0.9402859586706309
```

Information Gain of Attributes

```python
def information_gain(df, split_attribute_name, target_attribute_name, trac
e=0):
    print("Information Gain Calculation of ",split_attribute_name)

    '''
    Takes a DataFrame of attributes,and quantifies the entropy of a target
attribute after performing a split along the values of another attribute.
    '''

    # Split Data by Possible Vals of Attribute:
    df_split = df.groupby(split_attribute_name)
    #print(df_split.groups)
    for name,group in df_split:
        print(name)
        print(group)

    # Calculate Entropy for Target Attribute, as well as
    # Proportion of Obs in Each Data-Split
    nobs = len(df.index) * 1.0
    #print("NOBS",nobs)
    df_agg_ent = df_split.agg({target_attribute_name : [entropy_of_list, l
ambda x: len(x)/nobs] })[target_attribute_name]
    #print("DFAGGENT",df_agg_ent)
    df_agg_ent.columns = ['Entropy', 'PropObservations']
    #if trace: # helps understand what fxn is doing:
     #    print(df_agg_ent)

    # Calculate Information Gain:
    new_entropy = sum( df_agg_ent['Entropy'] * df_agg_ent['PropObservation
s'] )
    old_entropy = entropy_of_list(df[target_attribute_name])
```

```python
    return old_entropy - new_entropy


print('Info-gain for Outlook is :'+str( information_gain(df_tennis, 'Outlo
ok', 'PlayTennis')),"\n")
print('\n Info-gain for Humidity is: ' + str( information_gain(df_tennis,
'Humidity', 'PlayTennis')),"\n")
print('\n Info-gain for Wind is:' + str( information_gain(df_tennis, 'Wind
', 'PlayTennis')),"\n")
print('\n Info-gain for Temperature is:' + str( information_gain(df_tennis
, 'Temperature','PlayTennis')),"\n")
```

Output :

Information Gain Calculation of Outlook				
Overcast				
PlayTennis	Outlook	Temperature	Humidity	Wind
2 Yes	Overcast	Hot	High	Weak
6 Yes	Overcast	Cool	Normal	Strong
11 Yes	Overcast	Mild	High	Strong
12 Yes	Overcast	Hot	Normal	Weak
Rain				
PlayTennis	Outlook	Temperature	Humidity	Wind
3 Yes	Rain	Mild	High	Weak
4 Yes	Rain	Cool	Normal	Weak
5 No	Rain	Cool	Normal	Strong
9 Yes	Rain	Mild	Normal	Weak
13 No	Rain	Mild	High	Strong
Sunny				
PlayTennis	Outlook	Temperature	Humidity	Wind
0 No	Sunny	Hot	High	Weak
1 No	Sunny	Hot	High	Strong
7 No	Sunny	Mild	High	Weak
8 Yes	Sunny	Cool	Normal	Weak
10 Yes	Sunny	Mild	Normal	Strong
No and Yes Classes: PlayTennis Counter({'Yes': 4})				
No and Yes Classes: PlayTennis Counter({'Yes': 3, 'No': 2})				
No and Yes Classes: PlayTennis Counter({'No': 3, 'Yes': 2})				
No and Yes Classes: PlayTennis Counter({'Yes': 9, 'No': 5})				
Info-gain for Outlook is :0.246749819774				

Information Gain Calculation of Humidity				
High				
PlayTennis	Outlook	Temperature	Humidity	Wind

0	No	Sunny	Hot	High	Weak
1	No	Sunny	Hot	High	Strong
2	Yes	Overcast	Hot	High	Weak
3	Yes	Rain	Mild	High	Weak
7	No	Sunny	Mild	High	Weak
11	Yes	Overcast	Mild	High	Strong
13	No	Rain	Mild	High	Strong

Normal

	PlayTennis	Outlook	Temperature	Humidity	Wind
4	Yes	Rain	Cool	Normal	Weak
5	No	Rain	Cool	Normal	Strong
6	Yes	Overcast	Cool	Normal	Strong
8	Yes	Sunny	Cool	Normal	Weak
9	Yes	Rain	Mild	Normal	Weak
10	Yes	Sunny	Mild	Normal	Strong
12	Yes	Overcast	Hot	Normal	Weak

No and Yes Classes: PlayTennis Counter({'No': 4, 'Yes': 3})
No and Yes Classes: PlayTennis Counter({'Yes': 6, 'No': 1})
No and Yes Classes: PlayTennis Counter({'Yes': 9, 'No': 5})

Info-gain for Humidity is: 0.151835501362

Information Gain Calculation of Wind

Strong

	PlayTennis	Outlook	Temperature	Humidity	Wind
1	No	Sunny	Hot	High	Strong
5	No	Rain	Cool	Normal	Strong
6	Yes	Overcast	Cool	Normal	Strong
10	Yes	Sunny	Mild	Normal	Strong
11	Yes	Overcast	Mild	High	Strong
13	No	Rain	Mild	High	Strong

Weak

	PlayTennis	Outlook	Temperature	Humidity	Wind
0	No	Sunny	Hot	High	Weak
2	Yes	Overcast	Hot	High	Weak
3	Yes	Rain	Mild	High	Weak
4	Yes	Rain	Cool	Normal	Weak
7	No	Sunny	Mild	High	Weak
8	Yes	Sunny	Cool	Normal	Weak
9	Yes	Rain	Mild	Normal	Weak
12	Yes	Overcast	Hot	Normal	Weak

No and Yes Classes: PlayTennis Counter({'No': 3, 'Yes': 3})
No and Yes Classes: PlayTennis Counter({'Yes': 6, 'No': 2})
No and Yes Classes: PlayTennis Counter({'Yes': 9, 'No': 5})

Info-gain for Wind is:0.0481270304083				

```
Information Gain Calculation of  Temperature
Cool
   PlayTennis    Outlook Temperature Humidity    Wind
4      Yes       Rain        Cool    Normal     Weak
5      No        Rain        Cool    Normal    Strong
6      Yes    Overcast       Cool    Normal    Strong
8      Yes      Sunny        Cool    Normal     Weak
Hot
   PlayTennis    Outlook Temperature Humidity    Wind
0      No       Sunny         Hot     High      Weak
1      No       Sunny         Hot     High    Strong
2      Yes    Overcast        Hot     High      Weak
12     Yes    Overcast        Hot    Normal     Weak
Mild
   PlayTennis    Outlook Temperature Humidity    Wind
3      Yes       Rain        Mild     High      Weak
7      No       Sunny        Mild     High      Weak
9      Yes       Rain        Mild    Normal     Weak
10     Yes      Sunny        Mild    Normal    Strong
11     Yes    Overcast       Mild     High    Strong
13     No        Rain        Mild     High    Strong
No and Yes Classes: PlayTennis Counter({'Yes': 3, 'No': 1})
No and Yes Classes: PlayTennis Counter({'No': 2, 'Yes': 2})
No and Yes Classes: PlayTennis Counter({'Yes': 4, 'No': 2})
No and Yes Classes: PlayTennis Counter({'Yes': 9, 'No': 5})
```

Info-gain for Temperature is:0.029222565659				

ID3 Algorithm

```python
def id3(df, target_attribute_name, attribute_names, default_class=None):

    ## Tally target attribute:
    from collections import Counter
    cnt = Counter(x for x in df[target_attribute_name])# class of YES /NO

    ## First check: Is this split of the dataset homogeneous?
    if len(cnt) == 1:
        return next(iter(cnt))

    ## Second check: Is this split of the dataset empty?
    # if yes, return a default value
    elif df.empty or (not attribute_names):
```

```python
            return default_class

    ## Otherwise: This dataset is ready to be divvied up!
    else:
        # Get Default Value for next recursive call of this function:
        default_class = max(cnt.keys()) #[index_of_max] # most common valu
e of target attribute in dataset

        # Choose Best Attribute to split on:
        gainz = [information_gain(df, attr, target_attribute_name) for att
r in attribute_names]
        index_of_max = gainz.index(max(gainz))
        best_attr = attribute_names[index_of_max]

        # Create an empty tree, to be populated in a moment
        tree = {best_attr:{}}
        remaining_attribute_names = [i for i in attribute_names if i != be
st_attr]

        # Split dataset
        # On each split, recursively call this algorithm.
        # populate the empty tree with subtrees, which
        # are the result of the recursive call
        for attr_val, data_subset in df.groupby(best_attr):
            subtree = id3(data_subset,
                          target_attribute_name,
                          remaining_attribute_names,
                          default_class)
            tree[best_attr][attr_val] = subtree
        return tree
```

Predicting Attributes

```python
# Get Predictor Names (all but 'class')
attribute_names = list(df_tennis.columns)
print("List of Attributes:", attribute_names)
attribute_names.remove('PlayTennis') #Remove the class attribute
print("Predicting Attributes:", attribute_names)
```

Output :

List of Attributes: ['PlayTennis', 'Outlook', 'Temperature', 'Humidity', 'Wind']
Predicting Attributes: ['Outlook', 'Temperature', 'Humidity', 'Wind']

Tree Construction

In [85]:

```python
# Run Algorithm:
from pprint import pprint
tree = id3(df_tennis,'PlayTennis',attribute_names)
print("\n\nThe Resultant Decision Tree is :\n")
pprint(tree)
```

Output

Information Gain Calculation of Outlook					
Overcast					
	PlayTennis	Outlook	Temperature	Humidity	Wind
2	Yes	Overcast	Hot	High	Weak
6	Yes	Overcast	Cool	Normal	Strong
11	Yes	Overcast	Mild	High	Strong
12	Yes	Overcast	Hot	Normal	Weak
Rain					
	PlayTennis	Outlook	Temperature	Humidity	Wind
3	Yes	Rain	Mild	High	Weak
4	Yes	Rain	Cool	Normal	Weak
5	No	Rain	Cool	Normal	Strong
9	Yes	Rain	Mild	Normal	Weak
13	No	Rain	Mild	High	Strong
Sunny					
	PlayTennis	Outlook	Temperature	Humidity	Wind
0	No	Sunny	Hot	High	Weak
1	No	Sunny	Hot	High	Strong
7	No	Sunny	Mild	High	Weak
8	Yes	Sunny	Cool	Normal	Weak
10	Yes	Sunny	Mild	Normal	Strong
No and Yes Classes: PlayTennis Counter({'Yes': 4})					
No and Yes Classes: PlayTennis Counter({'Yes': 3, 'No': 2})					
No and Yes Classes: PlayTennis Counter({'No': 3, 'Yes': 2})					
No and Yes Classes: PlayTennis Counter({'Yes': 9, 'No': 5})					
Information Gain Calculation of Temperature					
Cool					
	PlayTennis	Outlook	Temperature	Humidity	Wind
4	Yes	Rain	Cool	Normal	Weak
5	No	Rain	Cool	Normal	Strong
6	Yes	Overcast	Cool	Normal	Strong
8	Yes	Sunny	Cool	Normal	Weak
Hot					
	PlayTennis	Outlook	Temperature	Humidity	Wind
0	No	Sunny	Hot	High	Weak
1	No	Sunny	Hot	High	Strong
2	Yes	Overcast	Hot	High	Weak
12	Yes	Overcast	Hot	Normal	Weak
Mild					
	PlayTennis	Outlook	Temperature	Humidity	Wind
3	Yes	Rain	Mild	High	Weak

7	No	Sunny	Mild	High	Weak
9	Yes	Rain	Mild	Normal	Weak
10	Yes	Sunny	Mild	Normal	Strong
11	Yes	Overcast	Mild	High	Strong
13	No	Rain	Mild	High	Strong

No and Yes Classes: PlayTennis Counter({'Yes': 3, 'No': 1})
No and Yes Classes: PlayTennis Counter({'No': 2, 'Yes': 2})
No and Yes Classes: PlayTennis Counter({'Yes': 4, 'No': 2})
No and Yes Classes: PlayTennis Counter({'Yes': 9, 'No': 5})
Information Gain Calculation of Humidity
High

	PlayTennis	Outlook	Temperature	Humidity	Wind
0	No	Sunny	Hot	High	Weak
1	No	Sunny	Hot	High	Strong
2	Yes	Overcast	Hot	High	Weak
3	Yes	Rain	Mild	High	Weak
7	No	Sunny	Mild	High	Weak
11	Yes	Overcast	Mild	High	Strong
13	No	Rain	Mild	High	Strong

Normal

	PlayTennis	Outlook	Temperature	Humidity	Wind
4	Yes	Rain	Cool	Normal	Weak
5	No	Rain	Cool	Normal	Strong
6	Yes	Overcast	Cool	Normal	Strong
8	Yes	Sunny	Cool	Normal	Weak
9	Yes	Rain	Mild	Normal	Weak
10	Yes	Sunny	Mild	Normal	Strong
12	Yes	Overcast	Hot	Normal	Weak

No and Yes Classes: PlayTennis Counter({'No': 4, 'Yes': 3})
No and Yes Classes: PlayTennis Counter({'Yes': 6, 'No': 1})
No and Yes Classes: PlayTennis Counter({'Yes': 9, 'No': 5})
Information Gain Calculation of Wind
Strong

	PlayTennis	Outlook	Temperature	Humidity	Wind
1	No	Sunny	Hot	High	Strong
5	No	Rain	Cool	Normal	Strong
6	Yes	Overcast	Cool	Normal	Strong
10	Yes	Sunny	Mild	Normal	Strong
11	Yes	Overcast	Mild	High	Strong
13	No	Rain	Mild	High	Strong

Weak

	PlayTennis	Outlook	Temperature	Humidity	Wind
0	No	Sunny	Hot	High	Weak
2	Yes	Overcast	Hot	High	Weak
3	Yes	Rain	Mild	High	Weak

4	Yes	Rain	Cool	Normal	Weak
7	No	Sunny	Mild	High	Weak
8	Yes	Sunny	Cool	Normal	Weak
9	Yes	Rain	Mild	Normal	Weak
12	Yes	Overcast	Hot	Normal	Weak

No and Yes Classes: PlayTennis Counter({'No': 3, 'Yes': 3})
No and Yes Classes: PlayTennis Counter({'Yes': 6, 'No': 2})
No and Yes Classes: PlayTennis Counter({'Yes': 9, 'No': 5})

Information Gain Calculation of Temperature

Cool

	PlayTennis	Outlook	Temperature	Humidity	Wind
4	Yes	Rain	Cool	Normal	Weak
5	No	Rain	Cool	Normal	Strong

Mild

	PlayTennis	Outlook	Temperature	Humidity	Wind
3	Yes	Rain	Mild	High	Weak
9	Yes	Rain	Mild	Normal	Weak
13	No	Rain	Mild	High	Strong

No and Yes Classes: PlayTennis Counter({'Yes': 1, 'No': 1})
No and Yes Classes: PlayTennis Counter({'Yes': 2, 'No': 1})
No and Yes Classes: PlayTennis Counter({'Yes': 3, 'No': 2})

Information Gain Calculation of Humidity

High

	PlayTennis	Outlook	Temperature	Humidity	Wind
3	Yes	Rain	Mild	High	Weak
13	No	Rain	Mild	High	Strong

Normal

	PlayTennis	Outlook	Temperature	Humidity	Wind
4	Yes	Rain	Cool	Normal	Weak
5	No	Rain	Cool	Normal	Strong
9	Yes	Rain	Mild	Normal	Weak

No and Yes Classes: PlayTennis Counter({'Yes': 1, 'No': 1})
No and Yes Classes: PlayTennis Counter({'Yes': 2, 'No': 1})
No and Yes Classes: PlayTennis Counter({'Yes': 3, 'No': 2})

Information Gain Calculation of Wind

Strong

	PlayTennis	Outlook	Temperature	Humidity	Wind
5	No	Rain	Cool	Normal	Strong
13	No	Rain	Mild	High	Strong

Weak

	PlayTennis	Outlook	Temperature	Humidity	Wind
3	Yes	Rain	Mild	High	Weak
4	Yes	Rain	Cool	Normal	Weak
9	Yes	Rain	Mild	Normal	Weak

No and Yes Classes: PlayTennis Counter({'No': 2})

No and Yes Classes: PlayTennis Counter({'Yes': 3})
No and Yes Classes: PlayTennis Counter({'Yes': 3, 'No': 2})
Information Gain Calculation of Temperature
Cool
PlayTennis Outlook Temperature Humidity Wind
8   Yes   Sunny   Cool   Normal Weak
Hot
PlayTennis Outlook Temperature Humidity   Wind
0   No Sunny   Hot   High   Weak
1   No Sunny   Hot   High Strong
Mild
PlayTennis Outlook Temperature Humidity   Wind
7   No Sunny   Mild   High   Weak
10   Yes   Sunny   Mild   Normal Strong
No and Yes Classes: PlayTennis Counter({'Yes': 1})
No and Yes Classes: PlayTennis Counter({'No': 2})
No and Yes Classes: PlayTennis Counter({'No': 1, 'Yes': 1})
No and Yes Classes: PlayTennis Counter({'No': 3, 'Yes': 2})
Information Gain Calculation of Humidity
High
PlayTennis Outlook Temperature Humidity   Wind
0   No Sunny   Hot   High   Weak
1   No Sunny   Hot   High Strong
7   No Sunny   Mild   High   Weak
Normal
PlayTennis Outlook Temperature Humidity   Wind
8   Yes   Sunny   Cool   Normal   Weak
10   Yes   Sunny   Mild   Normal Strong
No and Yes Classes: PlayTennis Counter({'No': 3})
No and Yes Classes: PlayTennis Counter({'Yes': 2})
No and Yes Classes: PlayTennis Counter({'No': 3, 'Yes': 2})
Information Gain Calculation of Wind
Strong
PlayTennis Outlook Temperature Humidity   Wind
1   No Sunny   Hot   High Strong
10   Yes   Sunny   Mild   Normal Strong
Weak
PlayTennis Outlook Temperature Humidity Wind
0   No Sunny   Hot   High   Weak
7   No Sunny   Mild   High   Weak
8   Yes   Sunny   Cool   Normal Weak
No and Yes Classes: PlayTennis Counter({'No': 1, 'Yes': 1})
No and Yes Classes: PlayTennis Counter({'No': 2, 'Yes': 1})
No and Yes Classes: PlayTennis Counter({'No': 3, 'Yes': 2})

The Resultant Decision Tree is :

{'Outlook': {'Overcast': 'Yes',
        'Rain': {'Wind': {'Strong': 'No', 'Weak': 'Yes'}},
        'Sunny': {'Humidity': {'High': 'No', 'Normal': 'Yes'}}}}

Classification Accuracy

```python
def classify(instance, tree, default=None):
    attribute = next(iter(tree))#tree.keys()[0]
    if instance[attribute] in tree[attribute].keys():
        result = tree[attribute][instance[attribute]]
        if isinstance(result, dict): # this is a tree, delve deeper
            return classify(instance, result)
        else:
            return result # this is a label
    else:
        return default
```

```python
df_tennis['predicted'] = df_tennis.apply(classify, axis=1, args=(tree,'No'
) )
    # classify func allows for a default arg: when tree doesn't have answe
r for a particular
    # combitation of attribute-values, we can use 'no' as the default gues
s

print('Accuracy is:' + str( sum(df_tennis['PlayTennis']==df_tennis['predic
ted'] ) / (1.0*len(df_tennis.index)) ))

df_tennis[['PlayTennis', 'predicted']]
```

Output :

Accuracy is:1.0

	PlayTennis	predicted
0	No	No
1	No	No
2	Yes	Yes
3	Yes	Yes
4	Yes	Yes
5	No	No
6	Yes	Yes
7	No	No
8	Yes	Yes
9	Yes	Yes
10	Yes	Yes
11	Yes	Yes
12	Yes	Yes
13	No	No

Classification Accuracy: Training/Testing Set

```python
training_data = df_tennis.iloc[1:-4] # all but last thousand instances
test_data    = df_tennis.iloc[-4:] # just the last thousand
train_tree = id3(training_data, 'PlayTennis', attribute_names)

test_data['predicted2'] = test_data.apply(
# <---- test_data source
                                          classify,
                                          axis=1,
                                          args=(train_tree,'Yes') ) # <---
- train_data tree


print ('\n\n Accuracy is : ' + str( sum(test_data['PlayTennis']==test_data
['predicted2'] ) / (1.0*len(test_data.index)) ))
```

Output :

```
Information Gain Calculation of  Outlook
```

Overcast						
	PlayTennis	Outlook	Temperature	Humidity	Wind	predicted
2	Yes	Overcast	Hot	High	Weak	Yes
6	Yes	Overcast	Cool	Normal	Strong	Yes
Rain						
	PlayTennis	Outlook	Temperature	Humidity	Wind	predicted
3	Yes	Rain	Mild	High	Weak	Yes
4	Yes	Rain	Cool	Normal	Weak	Yes
5	No	Rain	Cool	Normal	Strong	No
9	Yes	Rain	Mild	Normal	Weak	Yes
Sunny						
	PlayTennis	Outlook	Temperature	Humidity	Wind	predicted
1	No	Sunny	Hot	High	Strong	No
7	No	Sunny	Mild	High	Weak	No
8	Yes	Sunny	Cool	Normal	Weak	Yes
No and Yes Classes: PlayTennis Counter({'Yes': 2})						
No and Yes Classes: PlayTennis Counter({'Yes': 3, 'No': 1})						
No and Yes Classes: PlayTennis Counter({'No': 2, 'Yes': 1})						
No and Yes Classes: PlayTennis Counter({'Yes': 6, 'No': 3})						
Information Gain Calculation of Temperature						
Cool						
	PlayTennis	Outlook	Temperature	Humidity	Wind	predicted
4	Yes	Rain	Cool	Normal	Weak	Yes
5	No	Rain	Cool	Normal	Strong	No
6	Yes	Overcast	Cool	Normal	Strong	Yes
8	Yes	Sunny	Cool	Normal	Weak	Yes
Hot						
	PlayTennis	Outlook	Temperature	Humidity	Wind	predicted
1	No	Sunny	Hot	High	Strong	No
2	Yes	Overcast	Hot	High	Weak	Yes
Mild						
	PlayTennis	Outlook	Temperature	Humidity	Wind	predicted
3	Yes	Rain	Mild	High	Weak	Yes
7	No	Sunny	Mild	High	Weak	No
9	Yes	Rain	Mild	Normal	Weak	Yes
No and Yes Classes: PlayTennis Counter({'Yes': 3, 'No': 1})						
No and Yes Classes: PlayTennis Counter({'No': 1, 'Yes': 1})						
No and Yes Classes: PlayTennis Counter({'Yes': 2, 'No': 1})						
No and Yes Classes: PlayTennis Counter({'Yes': 6, 'No': 3})						
Information Gain Calculation of Humidity						
High						
	PlayTennis	Outlook	Temperature	Humidity	Wind	predicted
1	No	Sunny	Hot	High	Strong	No
2	Yes	Overcast	Hot	High	Weak	Yes
3	Yes	Rain	Mild	High	Weak	Yes

7	No	Sunny	Mild	High	Weak	No

Normal

	PlayTennis	Outlook	Temperature	Humidity	Wind	predicted
4	Yes	Rain	Cool	Normal	Weak	Yes
5	No	Rain	Cool	Normal	Strong	No
6	Yes	Overcast	Cool	Normal	Strong	Yes
8	Yes	Sunny	Cool	Normal	Weak	Yes
9	Yes	Rain	Mild	Normal	Weak	Yes

No and Yes Classes: PlayTennis Counter({'No': 2, 'Yes': 2})

No and Yes Classes: PlayTennis Counter({'Yes': 4, 'No': 1})

No and Yes Classes: PlayTennis Counter({'Yes': 6, 'No': 3})

Information Gain Calculation of Wind

Strong

	PlayTennis	Outlook	Temperature	Humidity	Wind	predicted
1	No	Sunny	Hot	High	Strong	No
5	No	Rain	Cool	Normal	Strong	No
6	Yes	Overcast	Cool	Normal	Strong	Yes

Weak

	PlayTennis	Outlook	Temperature	Humidity	Wind	predicted
2	Yes	Overcast	Hot	High	Weak	Yes
3	Yes	Rain	Mild	High	Weak	Yes
4	Yes	Rain	Cool	Normal	Weak	Yes
7	No	Sunny	Mild	High	Weak	No
8	Yes	Sunny	Cool	Normal	Weak	Yes
9	Yes	Rain	Mild	Normal	Weak	Yes

No and Yes Classes: PlayTennis Counter({'No': 2, 'Yes': 1})

No and Yes Classes: PlayTennis Counter({'Yes': 5, 'No': 1})

No and Yes Classes: PlayTennis Counter({'Yes': 6, 'No': 3})

Information Gain Calculation of Temperature

Cool

	PlayTennis	Outlook	Temperature	Humidity	Wind	predicted
4	Yes	Rain	Cool	Normal	Weak	Yes
5	No	Rain	Cool	Normal	Strong	No

Mild

	PlayTennis	Outlook	Temperature	Humidity	Wind	predicted
3	Yes	Rain	Mild	High	Weak	Yes
9	Yes	Rain	Mild	Normal	Weak	Yes

No and Yes Classes: PlayTennis Counter({'Yes': 1, 'No': 1})

No and Yes Classes: PlayTennis Counter({'Yes': 2})

No and Yes Classes: PlayTennis Counter({'Yes': 3, 'No': 1})

Information Gain Calculation of Humidity

High

	PlayTennis	Outlook	Temperature	Humidity	Wind	predicted
3	Yes	Rain	Mild	High	Weak	Yes

Normal

	PlayTennis	Outlook	Temperature	Humidity	Wind	predicted
4	Yes	Rain	Cool	Normal	Weak	Yes
5	No	Rain	Cool	Normal	Strong	No
9	Yes	Rain	Mild	Normal	Weak	Yes

No and Yes Classes: PlayTennis Counter({'Yes': 1})

No and Yes Classes: PlayTennis Counter({'Yes': 2, 'No': 1})

No and Yes Classes: PlayTennis Counter({'Yes': 3, 'No': 1})

Information Gain Calculation of Wind

Strong

	PlayTennis	Outlook	Temperature	Humidity	Wind	predicted
5	No	Rain	Cool	Normal	Strong	No

Weak

	PlayTennis	Outlook	Temperature	Humidity	Wind	predicted
3	Yes	Rain	Mild	High	Weak	Yes
4	Yes	Rain	Cool	Normal	Weak	Yes
9	Yes	Rain	Mild	Normal	Weak	Yes

No and Yes Classes: PlayTennis Counter({'No': 1})

No and Yes Classes: PlayTennis Counter({'Yes': 3})

No and Yes Classes: PlayTennis Counter({'Yes': 3, 'No': 1})

Information Gain Calculation of Temperature

Cool

	PlayTennis	Outlook	Temperature	Humidity	Wind	predicted
8	Yes	Sunny	Cool	Normal	Weak	Yes

Hot

	PlayTennis	Outlook	Temperature	Humidity	Wind	predicted
1	No	Sunny	Hot	High	Strong	No

Mild

	PlayTennis	Outlook	Temperature	Humidity	Wind	predicted
7	No	Sunny	Mild	High	Weak	No

No and Yes Classes: PlayTennis Counter({'Yes': 1})

No and Yes Classes: PlayTennis Counter({'No': 1})

No and Yes Classes: PlayTennis Counter({'No': 1})

No and Yes Classes: PlayTennis Counter({'No': 2, 'Yes': 1})

Information Gain Calculation of Humidity

High

	PlayTennis	Outlook	Temperature	Humidity	Wind	predicted
1	No	Sunny	Hot	High	Strong	No
7	No	Sunny	Mild	High	Weak	No

Normal

	PlayTennis	Outlook	Temperature	Humidity	Wind	predicted
8	Yes	Sunny	Cool	Normal	Weak	Yes

No and Yes Classes: PlayTennis Counter({'No': 2})

No and Yes Classes: PlayTennis Counter({'Yes': 1})

No and Yes Classes: PlayTennis Counter({'No': 2, 'Yes': 1})

Information Gain Calculation of Wind

```
Strong
  PlayTennis Outlook Temperature Humidity    Wind predicted
1        No   Sunny         Hot    High  Strong          No
Weak
  PlayTennis Outlook Temperature Humidity   Wind predicted
7        No   Sunny         Mild   High  Weak          No
8       Yes   Sunny         Cool  Normal  Weak         Yes
No and Yes Classes: PlayTennis Counter({'No': 1})
No and Yes Classes: PlayTennis Counter({'No': 1, 'Yes': 1})
No and Yes Classes: PlayTennis Counter({'No': 2, 'Yes': 1})
```

```
 Accuracy is : 0.75
```

Lab Exercise : Apply above Program to clasify the new sample /new data set.

Program4: Build an Artificial Neural Network by implementing the Backpropagation algorithm and test the same using appropriate data sets

Algorithm:

function BackProp $(D, \eta, n_{in}, n_{hidden}, n_{out})$

- D is the training set consists of m pairs: $\{(x_i, y_i)^m\}$
- η is the learning rate as an example (0.1)
- n_{in}, n_{hidden} e n_{out} are the numbero of imput hidden and output unit of neural network

Make a feed-forward network with n_{in}, n_{hidden} e n_{out} units
Initialize all the weight to short randomly number (es. [-0.05 0.05])
Repeat until termination condition are verifyed:
For any sample in D:

Forward propagate the network computing the output o_u of every unit u of the network
Back propagate the errors onto the network:
- For every output unit k, compute the error δ_k: $\delta_k = o_k(1-o_k)(t_k - o_k)$

- For every hidden unit h compute the error δ_h: $\delta_h = o_h(1-o_h) \sum_{k \in outputs} w_{kh} \delta_k$

- Update the network weight w_{ji}: $w_{ji} = w_{ji} + \Delta w_{ji},$ $where \ \Delta w_{ji} = \eta \delta_j x_{ji}$

(x_{ji} is the input of unit j from coming from unit i)

The Backpropagation Algorithm for a feed-forward 2-layer network of sigmoid units, the stochastic version

Idea: Gradient descent over the entire vector of network weights.

Initialize all weights to small random numbers.
Until satisfied, // *stopping criterion* to be (later) defined
    for each training example,

1. input the training example to the network, and compute the network outputs

2. for each output unit k:
   $\delta_k \leftarrow o_k(1 - o_k)(t_k - o_k)$

3. for each hidden unit h:
   $\delta_h \leftarrow o_h(1 - o_h) \sum_{k \in outputs} w_{kh}\delta_k$

4. update each network weight w_{ji}:
   $w_{ji} \leftarrow w_{ji} + \Delta w_{ji}$ where $\Delta w_{ji} = \eta\delta_j x_{ji}$,
   and x_{ji} is the ith input to unit j.

Source Code :

Below is a small contrived dataset that we can use to test out training our neural network.

X1	X2	Y
2.7810836	2.550537003	0
1.465489372	2.362125076	0
3.396561688	4.400293529	0
1.38807019	1.850220317	0
3.06407232	3.005305973	0
7.627531214	2.759262235	1
5.332441248	2.088626775	1
6.922596716	1.77106367	1
8.675418651	-0.242068655	1
7.673756466	3.508563011	1

Below is the complete example. We will use 2 neurons in the hidden layer. It is a binary classification problem (2 classes) so there will be two neurons in the output layer. The network will be trained for 20 epochs with a learning rate of 0.5, which is high because we are training for so few iterations.

```python
import random
from math import exp
from random import seed
# Initialize a network
def initialize_network(n_inputs, n_hidden, n_outputs):
    network = list()
    hidden_layer = [{'weights':[random.uniform(-0.5,0.5) for i in range(n_
inputs + 1)]} for i in range(n_hidden)]
    network.append(hidden_layer)
    output_layer = [{'weights':[random.uniform(-0.5,0.5) for i in range(n_
hidden + 1)]} for i in range(n_outputs)]
    network.append(output_layer)
    return network

# Calculate neuron activation for an input
def activate(weights, inputs):
    activation = weights[-1]
    for i in range(len(weights)-1):
        activation += weights[i] * inputs[i]
    return activation
```

```python
# Transfer neuron activation
def transfer(activation):
    return 1.0 / (1.0 + exp(-activation))

# Forward propagate input to a network output
def forward_propagate(network, row):
    inputs = row
    for layer in network:
        new_inputs = []
        for neuron in layer:
            activation = activate(neuron['weights'], inputs)
            neuron['output'] = transfer(activation)
            new_inputs.append(neuron['output'])
        inputs = new_inputs
    return inputs

# Calculate the derivative of an neuron output
def transfer_derivative(output):
    return output * (1.0 - output)

# Backpropagate error and store in neurons
def backward_propagate_error(network, expected):
    for i in reversed(range(len(network))):
        layer = network[i]
        errors = list()
        if i != len(network)-1:
            for j in range(len(layer)):
                error = 0.0
                for neuron in network[i + 1]:
                    error += (neuron['weights'][j] * neuron['delta'])
                errors.append(error)
        else:
            for j in range(len(layer)):
                neuron = layer[j]
                errors.append(expected[j] - neuron['output'])
        for j in range(len(layer)):
            neuron = layer[j]
            neuron['delta'] = errors[j] * transfer_derivative(neuron['output'])

# Update network weights with error
def update_weights(network, row, l_rate):
    for i in range(len(network)):
        inputs = row[:-1]
        if i != 0:
            inputs = [neuron['output'] for neuron in network[i - 1]]
        for neuron in network[i]:
            for j in range(len(inputs)):
                neuron['weights'][j] += l_rate * neuron['delta'] * inputs[j]
            neuron['weights'][-1] += l_rate * neuron['delta']

# Train a network for a fixed number of epochs
def train_network(network, train, l_rate, n_epoch, n_outputs):
```

```python
    for epoch in range(n_epoch):
        sum_error = 0
        for row in train:
            outputs = forward_propagate(network, row)
            expected = [0 for i in range(n_outputs)]
            expected[row[-1]] = 1
            sum_error += sum([(expected[i]-outputs[i])**2 for i in range(l
en(expected))])
            backward_propagate_error(network, expected)
            update_weights(network, row, l_rate)
        print('>epoch=%d, lrate=%.3f, error=%.3f' % (epoch, l_rate, sum_er
ror))

#Test training backprop algorithm
seed(1)
dataset = [[2.7810836,2.550537003,0],
    [1.465489372,2.362125076,0],
    [3.396561688,4.400293529,0],
    [1.38807019,1.850220317,0],
    [3.06407232,3.005305973,0],
    [7.627531214,2.759262235,1],
    [5.332441248,2.088626775,1],
    [6.922596716,1.77106367,1],
    [8.675418651,-0.242068655,1],
    [7.673756466,3.508563011,1]]
n_inputs = len(dataset[0]) - 1
n_outputs = len(set([row[-1] for row in dataset]))
network = initialize_network(n_inputs, 2, n_outputs)
train_network(network, dataset, 0.5, 20, n_outputs)

#for layer in network:
 #    print(layer)

i= 1
for layer in network:
    j=1
    for sub in layer:
        print("\n Layer[%d] Node[%d]:\n" %(i,j),sub)
        j=j+1
    i=i+1
```

Output :

```
>epoch=0, lrate=0.500, error=4.763
>epoch=1, lrate=0.500, error=4.558
>epoch=2, lrate=0.500, error=4.316
>epoch=3, lrate=0.500, error=4.035
>epoch=4, lrate=0.500, error=3.733
>epoch=5, lrate=0.500, error=3.428
>epoch=6, lrate=0.500, error=3.132
>epoch=7, lrate=0.500, error=2.850
>epoch=8, lrate=0.500, error=2.588
>epoch=9, lrate=0.500, error=2.348
```

```
>epoch=10, lrate=0.500, error=2.128
>epoch=11, lrate=0.500, error=1.931
>epoch=12, lrate=0.500, error=1.753
>epoch=13, lrate=0.500, error=1.595
>epoch=14, lrate=0.500, error=1.454
>epoch=15, lrate=0.500, error=1.329
>epoch=16, lrate=0.500, error=1.218
>epoch=17, lrate=0.500, error=1.120
>epoch=18, lrate=0.500, error=1.033
>epoch=19, lrate=0.500, error=0.956

 Layer[1] Node[1]:
 {'weights': [-1.435239043819221, 1.8587338175173547, 0.7917644224148094],
'output': 0.029795197360175857, 'delta': -0.006018730117768358}

 Layer[1] Node[2]:
 {'weights': [-0.7704959899742789, 0.8257894037467045, 0.21154103288579731
], 'output': 0.06771641538441577, 'delta': -0.005025585510232048}

 Layer[2] Node[1]:
 {'weights': [2.223584933362892, 1.2428928053374768, -1.3519548925527454],
'output': 0.23499833662766154, 'delta': -0.042246618795029306}

 Layer[2] Node[2]:
 {'weights': [-2.509732251870173, -0.5925943219491905, 1.259965727484093],
'output': 0.7543931062537561, 'delta': 0.04550706392557862}
```

Predict

Making predictions with a trained neural network is easy enough. We have already seen how to forward-propagate an input pattern to get an output. This is all we need to do to make a prediction. We can use the output values themselves directly as the probability of a pattern belonging to each output class. It may be more useful to turn this output back into a crisp class prediction. We can do this by selecting the class value with the larger probability. This is also called the arg max function. Below is a function named predict() that implements this procedure. It returns the index in the network output that has the largest probability. It assumes that class values have been converted to integers starting at 0.

```python
from math import exp

# Calculate neuron activation for an input
def activate(weights, inputs):
    activation = weights[-1]
    for i in range(len(weights)-1):
        activation += weights[i] * inputs[i]
    return activation
```

```python
# Transfer neuron activation
def transfer(activation):
    return 1.0 / (1.0 + exp(-activation))

# Forward propagate input to a network output
def forward_propagate(network, row):
    inputs = row
    for layer in network:
        new_inputs = []
        for neuron in layer:
            activation = activate(neuron['weights'], inputs)
            neuron['output'] = transfer(activation)
            new_inputs.append(neuron['output'])
        inputs = new_inputs
    return inputs

# Make a prediction with a network
def predict(network, row):
    outputs = forward_propagate(network, row)
    return outputs.index(max(outputs))

# Test making predictions with the network
dataset = [[2.7810836,2.550537003,0],
    [1.465489372,2.362125076,0],
    [3.396561688,4.400293529,0],
    [1.38807019,1.850220317,0],
    [3.06407232,3.005305973,0],
    [7.627531214,2.759262235,1],
    [5.332441248,2.088626775,1],
    [6.922596716,1.77106367,1],
    [8.675418651,-0.242068655,1],
    [7.673756466,3.508563011,1]]
network = [[{'weights': [-1.482313569067226, 1.8308790073202204, 1.0783819
22048799]}, {'weights': [0.23244990332399884, 0.3621998343835864, 0.402898
21191094327]}],
    [{'weights': [2.5001872433501404, 0.7887233511355132, -1.1026649757805
829]}, {'weights': [-2.429350576245497, 0.8357651039198697, 1.069921718128
0656]}]]
for row in dataset:
    prediction = predict(network, row)
    print('Expected=%d, Got=%d' % (row[-1], prediction))
```

```
Expected=0, Got=0
Expected=0, Got=0
Expected=0, Got=0
Expected=0, Got=0
Expected=0, Got=0
Expected=1, Got=1
Expected=1, Got=1
Expected=1, Got=1
Expected=1, Got=1
Expected=1, Got=1
```

Program5: Write a program to implement the **naïve Bayesian classifier** for a sample training data set stored as a .CSV file. Compute the accuracy of the classifier, considering few test data sets.

Bayesian Theorem:

$$P(h|D) = \frac{P(D|h)P(h)}{P(D)}$$

- $P(h)$ = prior probability of hypothesis h
- $P(D)$ = prior probability of training data D
- $P(h|D)$ = probability of h given D
- $P(D|h)$ = probability of D given h

$$\text{Posterior} = \frac{\text{Likelihood} \times \text{Prior}}{\text{Evidence}}$$

Naive Bayes: For the Bayesian Rule above, we have to extend it so that we have

$$P(C|X_1, X_2, ..., X_n) = \frac{P(X_1, X_2, ..., X_n|C)\ P(C)}{P(X_1, X_2, ..., X_n)}$$

Bayes' rule:

Given a set of variables, X = {x1,x2,x...,xd}, we want to construct the posterior probability for the event Cj among a set of possible outcomes C = {c1,c2,c...,cd} , the Bayes Rule is

$$p\left(C_j \mid x_1, x_2, \ldots, x_d\right) \propto p\left(x_1, x_2, \ldots, x_d \mid C_j\right) p\left(C_j\right)$$

Since Naive Bayes assumes that the conditional probabilities of the independent variables are statistically independent we can decompose the likelihood to a product of terms:

$$p\left(X \mid C_j\right) \propto \prod_{k=1}^{d} p\left(x_k \mid C_j\right)$$

and rewrite the posterior as:

$$p\left(C_j \mid X\right) \propto p\left(C_j\right) \prod_{k=1}^{d} p\left(x_k \mid C_j\right)$$

Using Bayes' rule above, we label a new case X with a class level Cj that achieves the highest posterior probability.

Naive Bayes can be modeled in several different ways including normal, lognormal, gamma and Poisson density functions:

$$p(x_k \mid C_j) = \begin{cases} \dfrac{1}{\sigma_{kj}\sqrt{2\pi}} \exp\left(\dfrac{-\left(x-\mu_{kj}\right)^2}{2\sigma_{kj}}\right), & -\infty < x < \infty, -\infty < \mu_{kj} <, \sigma_{kj} > 0 & \text{Normal} \\ \quad \mu_{kj} : \text{mean}, \ \sigma_{kj} : \text{standard deviation} \\[4pt] \dfrac{1}{x\sigma_{kj}(2\pi)^{1/2}} \exp\left\{\dfrac{-\left[\log\left(x/m_{kj}\right)\right]^2}{2\sigma_{kj}^2}\right\}, & 0 < x < \infty, m_{kj} > 0, \sigma_{kj} > 0 & \text{Lognormal} \\ \quad m_{kj} : \text{scale parameter}, \ \sigma_{kj} : \text{shape parameter} \\[4pt] \dfrac{\left(\dfrac{x}{b_{kj}}\right)^{c_{kj}-1}}{b_{kj}\Gamma\left(c_{kj}\right)} \exp\left(\dfrac{-x}{b_{kj}}\right), & 0 \le x < \infty, b_{kj} > 0, c_{kj} > 0 & \text{Gamma} \\ \quad b_{kj} : \text{scale parameter}, \ c_{kj} : \text{shape parameter} \\[4pt] \dfrac{\lambda_{kj} \exp\left(-\lambda_{kj}\right)}{x!}, & 0 \le x < \infty, \lambda_{kj} > 0, x = 0,1,2,\ldots & \text{Poisson} \\ \quad \lambda_{kj} : \text{mean} \end{cases}$$

Types

- **Gaussian:** It is used in classification and it assumes that features follow a normal distribution. Gaussian Naive Bayes is used in cases when all our features are continuous. For example in Iris dataset features are sepal width, petal width, sepal length, petal length.

$$P(x_i \mid y) = \frac{1}{\sqrt{2\pi\sigma_y^2}} \exp\left(-\frac{(x_i - \mu_y)^2}{2\sigma_y^2}\right)$$

- **Multinomial Naive Bayes :** Its is used when we have discrete data (e.g. movie ratings ranging 1 and 5 as each rating will have certain frequency to represent). In text learning we have the count of each word to predict the class or label

$$p(\mathbf{x} \mid C_k) = \frac{(\sum_i x_i)!}{\prod_i x_i!} \prod_i p_{ki}^{x_i}$$

$$\hat{P}(x_i \mid \omega_j) = \frac{\sum tf(x_i, d \in \omega_j) + \alpha}{\sum N_{d\in\omega j} + \alpha \cdot V}$$

- **Bernoulli Naive Bayes :** It assumes that all our features are binary such that they take only two values. Means 0s can represent "word does not occur in the document" and 1s as "word occurs in the document"

$$P(x_i \mid y) = P(i \mid y)x_i + (1 - P(i \mid y))(1 - x_i)$$

Source Code:

```python
# Example of Naive Bayes implemented from Scratch in Python
#http://machinelearningmastery.com/naive-bayes-classifier-scratch-python/
import csv
import random
import math

# 1.Data Handling
# 1.1 Loading the Data from csv file of Pima indians diabetes dataset.
def loadcsv(filename):
    lines = csv.reader(open(filename, "r"))
    dataset = list(lines)
    for i in range(len(dataset)):
        # converting the attributes from string to floating point numbers
        dataset[i] = [float(x) for x in dataset[i]]
    return dataset

#1.2 Splitting the Data set into Training Set
def splitDataset(dataset, splitRatio):
    trainSize = int(len(dataset) * splitRatio)
    trainSet = []
    copy = list(dataset)
    while len(trainSet) < trainSize:
        index = random.randrange(len(copy)) # random index
        trainSet.append(copy.pop(index))
    return [trainSet, copy]

#2.Summarize Data
#The naive bayes model is comprised of a
#summary of the data in the training dataset.
#This summary is then used when making predictions.
#involves the mean and the standard deviation for each attribute, by class
value

#2.1: Separate Data By Class
#Function to categorize the dataset in terms of classes
#The function assumes that the last attribute (-1) is the class value.
#The function returns a map of class values to lists of data instances.
def separateByClass(dataset):
    separated = {}
    for i in range(len(dataset)):
        vector = dataset[i]
        if (vector[-1] not in separated):
            separated[vector[-1]] = []
        separated[vector[-1]].append(vector)
    return separated

#The mean is the central middle or central tendency of the data,
# and we will use it as the middle of our gaussian distribution
# when calculating probabilities

#2.2 : Calculate Mean
```

```python
def mean(numbers):
    return sum(numbers)/float(len(numbers))

#The standard deviation describes the variation of spread of the data,
#and we will use it to characterize the expected spread of each attribute
#in our Gaussian distribution when calculating probabilities.

#2.3 : Calculate Standard Deviation
def stdev(numbers):
    avg = mean(numbers)
    variance = sum([pow(x-avg,2) for x in numbers])/float(len(numbers)-1)
    return math.sqrt(variance)

#2.4 : Summarize Dataset
#Summarize Data Set for a list of instances (for a class value)
#The zip function groups the values for each attribute across our data ins
tances
#into their own lists so that we can compute the mean and standard deviati
on values
#for the attribute.

def summarize(dataset):
    summaries = [(mean(attribute), stdev(attribute)) for attribute in zip(
*dataset)]
    del summaries[-1]
    return summaries

#2.5 : Summarize Attributes By Class
#We can pull it all together by first separating our training dataset into
#instances grouped by class.Then calculate the summaries for each attribut
e.

def summarizeByClass(dataset):
    separated = separateByClass(dataset)
    summaries = {}
    for classValue, instances in separated.items():
        summaries[classValue] = summarize(instances)
    return summaries

#3.Make Prediction
#3.1 Calculate Probaility Density Function
def calculateProbability(x, mean, stdev):
    exponent = math.exp(-(math.pow(x-mean,2)/(2*math.pow(stdev,2))))
    return (1 / (math.sqrt(2*math.pi) * stdev)) * exponent

#3.2 Calculate Class Probabilities
def calculateClassProbabilities(summaries, inputVector):
    probabilities = {}
    for classValue, classSummaries in summaries.items():
        probabilities[classValue] = 1
        for i in range(len(classSummaries)):
            mean, stdev = classSummaries[i]
            x = inputVector[i]
```

```python
            probabilities[classValue] *= calculateProbability(x, mean, std
ev)
    return probabilities

#3.3 Prediction : look for the largest probability and return the associat
ed class
def predict(summaries, inputVector):
    probabilities = calculateClassProbabilities(summaries, inputVector)
    bestLabel, bestProb = None, -1
    for classValue, probability in probabilities.items():
        if bestLabel is None or probability > bestProb:
            bestProb = probability
            bestLabel = classValue
    return bestLabel

#4.Make Predictions
# Function which return predictions for list of predictions
# For each instance

def getPredictions(summaries, testSet):
    predictions = []
    for i in range(len(testSet)):
        result = predict(summaries, testSet[i])
        predictions.append(result)
    return predictions

#5. Computing Accuracy
def getAccuracy(testSet, predictions):
    correct = 0
    for i in range(len(testSet)):
        if testSet[i][-1] == predictions[i]:
            correct += 1
    return (correct/float(len(testSet))) * 100.0

#Main Function
def main():
    filename = 'C:\\Users\\Dr.Thyagaraju\\Desktop\\Data\\pima-indians-diab
etes.csv'
    splitRatio = 0.67
    dataset = loadcsv(filename)

    #print("\n The Data Set :\n",dataset)
    print("\n The length of the Data Set : ",len(dataset))

    print("\n The Data Set Splitting into Training and Testing \n")
    trainingSet, testSet = splitDataset(dataset, splitRatio)

    print('\n Number of Rows in Training Set:{0} rows'.format(len(training
Set)))
    print('\n Number of Rows in Testing Set:{0} rows'.format(len(testSet))
)

    print("\n First Five Rows of Training Set:\n")
    for i in range(0,5):
```

```
            print(trainingSet[i],"\n")

      print("\n First Five Rows of Testing Set:\n")
      for i in range(0,5):
            print(testSet[i],"\n")

      # prepare model
      summaries = summarizeByClass(trainingSet)
      print("\n Model Summaries:\n",summaries)

      # test model
      predictions = getPredictions(summaries, testSet)
      print("\nPredictions:\n",predictions)

      accuracy = getAccuracy(testSet, predictions)
      print('\n Accuracy: {0}%'.format(accuracy))
main()
```

Output:

```
The length of the Data Set :  768

 The Data Set Splitting into Training and Testing

 Number of Rows in Training Set:514 rows
 Number of Rows in Testing Set:254 rows
 First Five Rows of Training Set:

[4.0, 116.0, 72.0, 12.0, 87.0, 22.1, 0.463, 37.0, 0.0]
[0.0, 84.0, 64.0, 22.0, 66.0, 35.8, 0.545, 21.0, 0.0]
[0.0, 162.0, 76.0, 36.0, 0.0, 49.6, 0.364, 26.0, 1.0]
[10.0, 101.0, 86.0, 37.0, 0.0, 45.6, 1.136, 38.0, 1.0]
[5.0, 78.0, 48.0, 0.0, 0.0, 33.7, 0.654, 25.0, 0.0]
```

First Five Rows of Testing Set:

```
[1.0, 85.0, 66.0, 29.0, 0.0, 26.6, 0.351, 31.0, 0.0]
[8.0, 183.0, 64.0, 0.0, 0.0, 23.3, 0.672, 32.0, 1.0]
[4.0, 110.0, 92.0, 0.0, 0.0, 37.6, 0.191, 30.0, 0.0]
[10.0, 139.0, 80.0, 0.0, 0.0, 27.1, 1.441, 57.0, 0.0]
[7.0, 100.0, 0.0, 0.0, 0.0, 30.0, 0.484, 32.0, 1.0]
```

Model Summaries:

```
 {0.0: [(3.3474320241691844, 3.045635385378286), (111.54380664652568, 26.0
40069054720693), (68.45921450151057, 18.15540652389224), (19.9456193353474
3, 14.709615608767137), (71.50151057401813, 101.04863439385403), (30.86314
1993957708, 7.207208162103949), (0.4341842900302116, 0.2960911906946818),
(31.613293051359516, 12.100651311117689)], 1.0: [(4.469945355191257, 3.736
9440851983082), (139.3879781420765, 33.733070931373234), (71.1475409836065
6, 20.694403393963842), (22.92896174863388, 18.151995092528765), (107.9781
```

```
4207650273, 146.92526156736633), (35.28633879781422, 7.783342260348583), (
0.5569726775956286, 0.3942245334398509), (36.78688524590164, 11.1746102827
02282)]}
```

Predictions:
```
 [0.0, 1.0, 0.0, 1.0, 0.0, 1.0, 1.0, 1.0, 0.0, 0.0, 1.0, 0.0, 1.0, 1.0, 0.
0, 0.0, 0.0, 1.0, 1.0, 1.0, 0.0, 1.0, 0.0, 1.0, 0.0, 1.0, 1.0, 0.0, 0.0, 0
.0, 0.0, 0.0, 1.0, 0.0, 0.0, 0.0, 0.0, 1.0, 1.0, 1.0, 0.0, 0.0, 0.0, 0.0,
1.0, 1.0, 1.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 1.0, 0.0, 1.0, 0.0, 0.0, 0.0,
1.0, 1.0, 0.0, 0.0, 1.0, 0.0, 0.0, 0.0, 1.0, 1.0, 0.0, 0.0, 1.0, 1.0, 1.0,
1.0, 0.0, 0.0, 0.0, 1.0, 1.0, 0.0, 0.0, 0.0, 1.0, 0.0, 1.0, 1.0, 0.0, 0.0,
0.0, 0.0, 0.0, 0.0, 1.0, 0.0, 0.0, 0.0, 1.0, 0.0, 0.0, 1.0, 0.0, 1.0, 0.0,
1.0, 1.0, 0.0, 0.0, 0.0, 1.0, 0.0, 0.0, 1.0, 1.0, 1.0, 1.0, 0.0, 1.0, 0.0,
0.0, 0.0, 0.0, 1.0, 1.0, 0.0, 0.0, 0.0, 1.0, 0.0, 0.0, 0.0, 0.0, 1.0, 0.0,
1.0, 0.0, 0.0, 0.0, 0.0, 1.0, 1.0, 0.0, 0.0, 1.0, 0.0, 1.0, 1.0, 0.0, 0.0,
0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 1.0, 0.0, 0.0, 0.0, 0.0, 0.0, 1.0, 0.0, 0.0,
0.0, 1.0, 1.0, 0.0, 0.0, 1.0, 0.0, 0.0, 0.0, 1.0, 1.0, 0.0, 0.0, 1.0, 0.0,
0.0, 0.0, 0.0, 0.0, 1.0, 0.0, 0.0, 0.0, 0.0, 0.0, 1.0, 0.0, 1.0, 1.0, 0.0,
0.0, 1.0, 0.0, 0.0, 0.0, 1.0, 0.0, 1.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0,
1.0, 0.0, 0.0, 1.0, 1.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 1.0, 0.0, 0.0, 1.0,
1.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 1.0, 1.0, 1.0, 0.0, 1.0, 0.0,
0.0, 0.0, 0.0, 1.0, 1.0, 1.0, 1.0, 1.0, 1.0, 0.0, 1.0, 0.0, 0.0, 1.0, 0.0]
```

Accuracy: 80.31496062992126%

Program6: Assuming a set of documents that need to be classified, use the naïve Bayesian Classifier model to perform this task. Built-in Java classes/API can be used to write the program. Calculate the accuracy, precision, and recall for your data set.

Algorithm :

Learning to Classify Text: Preliminaries

Target concept Interesting? : $Document \rightarrow \{+, -\}$
1. Represent each document by vector of words
- one attribute per word position in document

2. Learning: Use training examples to estimate
- $P(+)$ – $P(-)$
- $P(doc|+)$ – $P(doc|-)$

Naive Bayes conditional independence assumption

$$P(doc|v_j) = \prod_{i=1}^{length(doc)} P(a_i = w_k|v_j)$$

where $P(a_i = w_k \mid v_j)$ is probability that word in position i is w_k, given v_j
one more assumption:

$$P(a_i = w_k|v_j) = P(a_m = w_k|v_j), \forall i, m$$

Learning to Classify Text: Algorithm

S1: LEARN_NAIVE_BAYES_TEXT (*Examples*, V)
S2: CLASSIFY_NAIVE_BAYES_TEXT (*Doc*)
- *Examples is a set of text documents along with their target values. V is the set of all possible target values. This function learns the probability terms P(wk Iv,), describing the probability that a randomly drawn word from a document in class vj will be the English word wk. It also learns the class prior probabilities P(vj).*

S1: LEARN_NAIVE_BAYES_TEXT (*Examples*, V)

1. *collect all words and other tokens that occur in Examples*
- *Vocabulary ← all distinct words and other tokens in Examples*

2. *calculate the required P(vⱼ) and P(wₖ | vⱼ) probability terms*
- For each target value v_j in *V* do

$$P(v_j) \leftarrow \frac{|docs_j|}{|Examples|}$$

- ○ **$docs_j$ ← subset of *Examples* for which the target value is v_j**
- ○ $Text_j$ ← a single document created by concatenating all members of $docs_j$
- n ← total number of words in $Text_j$ (counting duplicate words multiple times)
- for each word w_k in *Vocabulary*
  - * n_k ← number of times word w_k occurs in $Text_j$

$$P(w_k|v_j) \leftarrow \frac{n_k+1}{n+|Vocabulary|}$$

S2: CLASSIFY_NAIVE_BAYES_TEXT (*Doc*)

- *positions ←* all word positions in *Doc* that contain tokens found in *Vocabulary*
- Return v_{NB} where

$$v_{NB} = \operatorname*{argmax}_{v_j \in V} P(v_j) \prod_{i \in positions} P(a_i|v_j)$$

Twenty News Groups

- Given 1000 training documents from each group Learn to classify new documents according to which newsgroup it came from

comp.graphics	misc.forsale	alt.atheism	sci.space
comp.os.ms-windows.misc	rec.autos	soc.religion.christian	sci.crypt
comp.sys.ibm.pc.hardware	rec.motorcycles	talk.religion.misc	sci.electronics
comp.sys.mac.hardware	rec.sport.baseball	talk.politics.mideast	sci.med
comp.windows.x	rec.sport.hockey	talk.politics.misc	
		talk.politics.guns	

- Naive Bayes: 89% classification accuracy
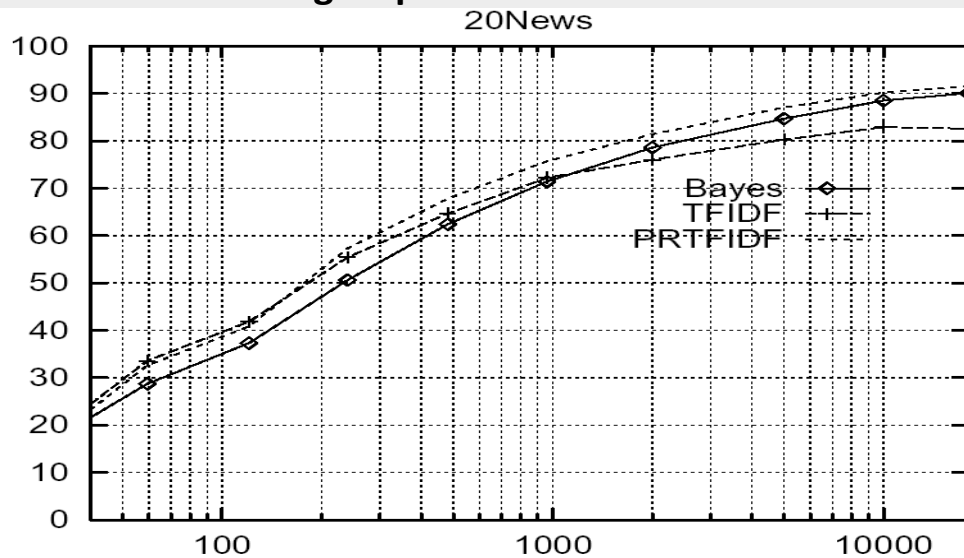
Learning Curve for 20 Newsgroups

Fig: Accuracy vs. Training set size (1/3 withheld for test

Example :

- In the example, we are given a sentence " A very close game", a training set of five sentences (as shown below), and their corresponding category (Sports or Not Sports).
- The goal is to build a Naive Bayes classifier that will tell us which category the sentence " A very close game" belongs to. applying a Naive Bayes classifier, thus the strategy would be calculating the probability of both "A very close game is Sports", as well as it's *Not Sports.* The one with the higher probability will be the result.
- to calculate P(*Sports | A very close game*), i.e. the probability that the category of the sentence is *Sports*given that the sentence is "A very close game".

Text	Category
"A great game"	Sports
"The election was over"	Not sports
"Very clean match"	Sports
"A clean but forgettable game"	Sports
"It was a close election"	Not sports

Step 1: Feature Engineering

- word frequencies, i.e., counting the occurrence of every word in the document.
- *P(a very close game)* = P(a)XP(very)XP(close)XP(game)
- *P(a very close game | Sports)* = P(a|Sports) X P(Very|Sports) X P(close|Sports) X P(game|Sports)
- P(*a very close game | Not Sports*) = P(*a | Not Sports*) x P(*very | Not Sports*) x P(*close | Not Sports*) x P(*game | Not Sports*)

Step 2: Calculating the probabilities

- Here , the word "close" does not exist in the category Sports, thus P(*close |Sports*) = 0, leading to P(*a very close game | Sports*)=0.
- Given an observation x = (x1, ..., xd) from a multinomial distribution with N trials and parameter vector θ = (θ1, ..., θd), a "smoothed" version of the data gives the estimator.

$$\hat{\theta}_i = \frac{x_i + \alpha}{N + \alpha d} \qquad (i = 1, \ldots, d),$$

- where the pseudo count α > 0 is the smoothing parameter (α = 0 corresponds to no smoothing)

Word	P(word | Sports)	P(word | Not Sports)
a	$\dfrac{2 + 1}{11 + 14}$	$\dfrac{1 + 1}{9 + 14}$
very	$\dfrac{1 + 1}{11 + 14}$	$\dfrac{0 + 1}{9 + 14}$
close	$\dfrac{0 + 1}{11 + 14}$	$\dfrac{1 + 1}{9 + 14}$
game	$\dfrac{2 + 1}{11 + 14}$	$\dfrac{0 + 1}{9 + 14}$

$P(a|Sports) \times P(very|Sports) \times P(close|Sports) \times P(game|Sports) \times P(Sports)$
$= 4.61 \times 10^{-5}$
$= 0.0000461$

$P(a - Not\ Sports) \times P(very|Not\ Sports) \times P(close|Not\ Sports) \times P(game|Not\ Sports) \times P(Not\ Sports)$
$= 1.43 \times 10^{-5}$
$= 0.0000143$

As seen from the results shown below, P(a very close game | Sports) gives a higher probability, suggesting that the sentence belongs to the Sports category.

Multinomial Naive Bayes

Term Frequency

A alternative approach to characterize text documents — rather than binary values — is the *term frequency (tf(t, d))*. The term frequency is typically defined as the number of times a given term *t* (i.e., word or token) appears in a document *d* (this approach is sometimes also called *raw frequency*). In practice, the term frequency is often normalized by dividing the raw term frequency by the document length.

$$\text{normalized term frequency} = \frac{tf(t,d)}{n_d}$$

where

- $tf(t,d)$: Raw term frequency (the count of term t in document d).
- n_d: The total number of terms in document d.

The term frequencies can then be used to compute the maximum-likelihood estimate based on the training data to estimate the class-conditional probabilities in the multinomial model:

$$\hat{P}(x_i \mid \omega_j) = \frac{\sum tf(x_i, d \in \omega_j) + \alpha}{\sum N_{d \in \omega j} + \alpha \cdot V}$$

where

- x_i: A word from the feature vector $\mathbf{x}$ of a particular sample.
- $\sum tf(x_i, d \in \omega_j)$: The sum of raw term frequencies of word x_i from all documents in the training sample that belong to class ω_j.
- $\sum N_{d \in \omega j}$: The sum of all term frequencies in the training dataset for class ω_j.
- α: An additive smoothing parameter ($\alpha = 1$ for Laplace smoothing).
- V: The size of the vocabulary (number of different words in the training set).

The class-conditional probability of encountering the text $\mathbf{x}$ can be calculated as the product from the likelihoods of the individual words (under the *naive* assumption of conditional independence).

$$P(\mathbf{x} \mid \omega_j) = P(x_1 \mid \omega_j) \cdot P(x_2 \mid \omega_j) \cdot \ldots \cdot P(x_n \mid \omega_j) = \prod^{m} P(x_i \mid \omega_j)$$

Source Code :

Loading the 20 newsgroups dataset : The dataset is called "Twenty Newsgroups". Here is the official description, quoted from the website:http://qwone.com/~jason/20Newsgroups/

The 20 Newsgroups data set is a collection of approximately 20,000 newsgroup documents, partitioned (nearly) evenly across 20 different newsgroups. To the best of our knowledge, it was originally collected by Ken Lang, probably for his paper "Newsweeder: Learning to filter netnews," though he does not explicitly mention this collection. The 20 newsgroups collection has become a popular data set for experiments in text applications of machine learning techniques, such as text classification and text clustering.

```python
from sklearn.datasets import fetch_20newsgroups
twenty_train = fetch_20newsgroups(subset='train', shuffle=True)
x = len(twenty_train.target_names)
print("\n The number of categories:",x)
print("\n The %d Different Categories of 20Newsgroups\n" %x)
i=1
for cat in twenty_train.target_names:
    print("Category[%d]:" %i,cat)
    i=i+1
print("\n Length of training data is",len(twenty_train.data))
print("\n Length of file names is ",len(twenty_train.filenames))

print("\n The Content/Data of First File is :\n")

print(twenty_train.data[0])


print("\n The Contents/Data of First 10 Files is in Training Data :\n")

for i in range(0,10):
    print("\n FILE NO:%d \n"%(i+1))
    print(twenty_train.data[i])
```

Considering only four Categories

```python
categories = ['alt.atheism', 'soc.religion.christian','comp.graphics', 'sci.med']
twenty_train = fetch_20newsgroups(subset='train',     categories=categories, shuffle=True, random_state=42)
print("\n Reduced Target Names:\n",twenty_train.target_names)
print("\n Reduced Target Length:\n", len(twenty_train.data))
print("\nFirst Document : ",twenty_train.data[0])
```

Extracting features from text files

Word Occurrences

```python
from sklearn.feature_extraction.text import CountVectorizer
count_vect = CountVectorizer()
X_train_counts = count_vect.fit_transform(twenty_train.data)
```

```
print("\n(Target Length , Distinct Words):",X_train_counts.shape)
print("\n Frequency of the word algorithm:", count_vect.vocabulary_.get('a
lgorithm'))
```

From occurrences to frequencies

```
(Target Length , Distinct Words): (2257, 35788)

 Frequency of the word algorithm: 4690
```

From occurrences to frequencies

Term Frequencies : Divide the number of occurrences of each word in a document by the total number of words in the document: these new features are called tf for Term Frequencies. Another refinement on top of tf is to downscale weights for words that occur in many documents in the corpus and are therefore less informative than those that occur only in a smaller portion of the corpus.This downscaling is called tf–idf for "Term Frequency times Inverse Document Frequency". Both tf and tf–idf can be computed as follows:

```
from sklearn.feature_extraction.text import TfidfTransformer
tf_transformer = TfidfTransformer(use_idf=False).fit(X_train_counts)
X_train_tf = tf_transformer.transform(X_train_counts)
X_train_tf.shape
(2257, 35788)
```

In the above example-code, we firstly use the fit(..) method to fit our estimator to the data and secondly the transform(..) method to transform our count-matrix to a tf-idf representation. These two steps can be combined to achieve the same end result faster by skipping redundant processing. This is done through using the fit_transform(..) method as shown below, and as mentioned in the note in the previous section:

```
tfidf_transformer = TfidfTransformer()
X_train_tfidf = tfidf_transformer.fit_transform(X_train_counts)
X_train_tfidf.shape
(2257, 35788)
```

Now that we have our features, we can train a classifier to try to predict the category of a post. Let's start with a naïve Bayes classifier, which provides a nice baseline for this task. scikit-learn includes several variants of this classifier; the one most suitable for word counts is the multinomial variant:

Training a classifier

```
from sklearn.naive_bayes import MultinomialNB
clf = MultinomialNB().fit(X_train_tfidf, twenty_train.target)
```

Predicting the Outcome

To try to predict the outcome on a new document we need to extract the features using almost the same feature extracting chain as before. The difference is that we call transform instead of fit_transform on the transformers, since they have already been fit to the training set:

```
docs_new = ['God is love', 'OpenGL on the GPU is fast']
X_new_counts = count_vect.transform(docs_new)
X_new_tfidf = tfidf_transformer.transform(X_new_counts)
```

```
predicted = clf.predict(X_new_tfidf)


for doc, category in zip(docs_new, predicted):
    print('%r => %s' % (doc, twenty_train.target_names[category]))
'God is love' => soc.religion.christian
'OpenGL on the GPU is fast' => comp.graphics
```

Building a pipeline

In order to make the vectorizer => transformer => classifier easier to work with, scikit-learn provides a Pipeline class that behaves like a compound classifier:

```
from sklearn.pipeline import Pipeline
text_clf = Pipeline([('vect', CountVectorizer()),
                     ('tfidf', TfidfTransformer()),
                     ('clf', MultinomialNB()),
 ])
```

The names vect, tfidf and clf (classifier) are arbitrary. We shall see their use in the section on grid search, below. We can now train the model with a single command:

```
text_clf.fit(twenty_train.data, twenty_train.target)
Pipeline(memory=None,
     steps=[('vect', CountVectorizer(analyzer='word', binary=False, decode_er
ror='strict',
        dtype=<class 'numpy.int64'>, encoding='utf-8', input='content',
        lowercase=True, max_df=1.0, max_features=None, min_df=1,
        ngram_range=(1, 1), preprocessor=None, stop_words=None,
        strip...inear_tf=False, use_idf=True)), ('clf', MultinomialNB(alpha=1
.0, class_prior=None, fit_prior=True))])
```


Evaluation of the performance on the test set

```
#Evaluating the predictive accuracy of the model is equally easy:
import numpy as np
twenty_test = fetch_20newsgroups(subset='test',categories=categories, shuffle
=True, random_state=42)
docs_test = twenty_test.data
predicted = text_clf.predict(docs_test)
np.mean(predicted == twenty_test.target)
0.83488681757656458
```

scikit-learn further provides utilities for more detailed performance analysis of the results:

```
from sklearn import metrics
print(metrics.classification_report(twenty_test.target, predicted,
    target_names=twenty_test.target_names))
                    precision    recall  f1-score   support
```

```
          alt.atheism        0.97      0.60      0.74       319
       comp.graphics        0.96      0.89      0.92       389
             sci.med        0.97      0.81      0.88       396
soc.religion.christian       0.65      0.99      0.78       398

          avg / total        0.88      0.83      0.84      1502
```

```
metrics.confusion_matrix(twenty_test.target, predicted)
array([[192,   2,   6, 119],
       [  2, 347,   4,  36],
       [  2,  11, 322,  61],
       [  2,   2,   1, 393]], dtype=int64)
```

As expected the confusion matrix shows that posts from the newsgroups on atheism and christian are more often confused for one another than with computer graphics.

```
Reference : http://scikit-learn.org/stable/tutorial/text_analytics/working_wi
th_text_data.html
```

Program7 : Write a program to construct a **Bayesian network** considering medical data. Use this model to demonstrate the diagnosis of heart patients using standard Heart Disease Data Set. You can use Java/Python ML library classes/API.

Algorithm :

Bayesian Network (BAYESIAN BELIEF NETWORKS

- Bayesian Belief networks describe conditional independence among *subsets* of variables
  → allows combining prior knowledge about (in)dependencies among variables with observed training data (also called Bayes Nets)

Conditional Independence

- Definition: *X* is *conditionally independent* of *Y* given *Z* if the probability distribution governing *X* is independent of the value of *Y* given the value of *Z*; that is, if
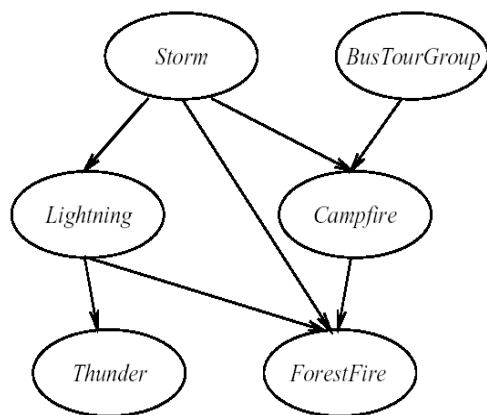 $$(\forall x_i, y_j, z_k)\ P(X= x_i | Y= y_j, Z= z_k) = P(X= x_i | Z= z_k)$$
  more compactly, we write
  $$P(X|Y, Z) = P(X|Z)$$
- Example: *Thunder* is conditionally independent of *Rain*, given *Lightning*
  $$P(Thunder|Rain, Lightning) = P(Thunder|Lightning)$$
- Naive Bayes uses cond. indep. to justify
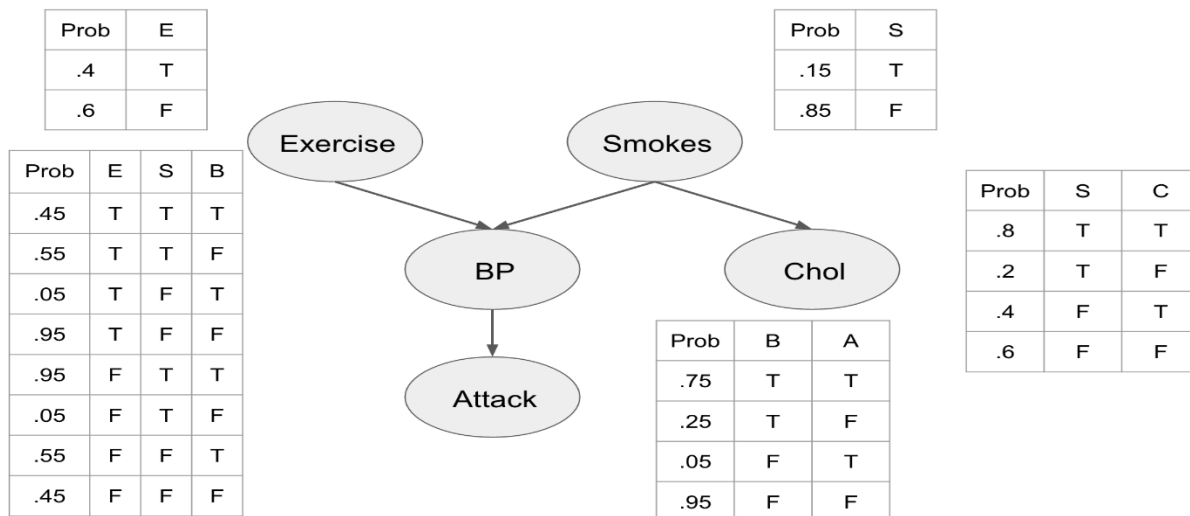 $$P(X, Y|Z) = P(X|Y, Z)\ P(Y|Z) = P(X|Z)\ P(Y|Z)$$

Bayesian Belief Network

	S,B	S,¬B	¬S,B	¬S,¬B
C	0.4	0.1	0.8	0.2
¬C	0.6	0.9	0.2	0.8

- Represents a set of conditional independence assertions:
  - Each node is asserted to be conditionally independent of its non descendants, given its immediate predecessors.
  - Directed acyclic graph

- Represents joint probability distribution over all variables
  - e.g., P(*Storm, BusTourGroup, . . . , ForestFire*)
  - in general,

$$P(y_1, \ldots, y_n) = \prod_{i=1}^{n} P(y_i | Parents(Y_i))$$

  where *Parents(Y$_i$)* denotes immediate predecessors of *Y$_i$* in graph
  - so, joint distribution is fully defined by graph, plus the P(*y$_i$|Parents(Y$_i$)*)

Example 1:

Prob	E
.4	T
.6	F

Prob	S
.15	T
.85	F

Prob	E	S	B
.45	T	T	T
.55	T	T	F
.05	T	F	T
.95	T	F	F
.95	F	T	T
.05	F	T	F
.55	F	F	T
.45	F	F	F

Prob	S	C
.8	T	T
.2	T	F
.4	F	T
.6	F	F

Exercise   Smokes

BP   Chol

Prob	B	A
.75	T	T
.25	T	F
.05	F	T
.95	F	F

Attack

Example2 :

Pollution   Smoker

P(S=T)
0.30

P(P=L)
0.90

Cancer

P	S	P(C=T|P,S)
H	T	0.05
H	F	0.02
L	T	0.03
L	F	0.001

XRay   Dyspnoea

C	P(X=pos|C)
T	0.90
F	0.20

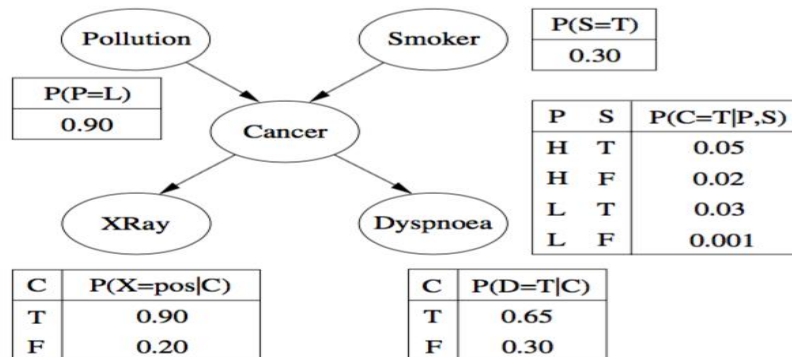| C	P(D=T|C)
T	0.65
F	0.30

FIGURE 2.1
A BN for the lung cancer problem.

Source Code :

7.1. Constructing a Bayesian Network considering Medical Data
7.1.1 Defining a Structure with nodes and edges

```python
# Starting with defining the network structure
from pgmpy.models import BayesianModel

cancer_model = BayesianModel([('Pollution', 'Cancer'),
                              ('Smoker', 'Cancer'),
                              ('Cancer', 'Xray'),
                              ('Cancer', 'Dyspnoea')])
cancer_model.nodes()

cancer_model.edges()

cancer_model.get_cpds()
```

7.1.2 Creation of Conditional Probability Table

```python
# Now defining the parameters.
from pgmpy.factors.discrete import TabularCPD

cpd_poll = TabularCPD(variable='Pollution', variable_card=2,
                      values=[[0.9], [0.1]])
cpd_smoke = TabularCPD(variable='Smoker', variable_card=2,
                      values=[[0.3], [0.7]])
cpd_cancer = TabularCPD(variable='Cancer', variable_card=2,
                      values=[[0.03, 0.05, 0.001, 0.02],
                              [0.97, 0.95, 0.999, 0.98]],
                      evidence=['Smoker', 'Pollution'],
                      evidence_card=[2, 2])
cpd_xray = TabularCPD(variable='Xray', variable_card=2,
                      values=[[0.9, 0.2], [0.1, 0.8]],
                      evidence=['Cancer'], evidence_card=[2])
cpd_dysp = TabularCPD(variable='Dyspnoea', variable_card=2,
                      values=[[0.65, 0.3], [0.35, 0.7]],
                      evidence=['Cancer'], evidence_card=[2])
```

7.1.3 Associating Conditional probabilities with the Bayesian Structure

```python
# Associating the parameters with the model structure.
cancer_model.add_cpds(cpd_poll, cpd_smoke, cpd_cancer, cpd_xray, cpd_dysp)

# Checking if the cpds are valid for the model.
cancer_model.check_model()

# Doing some simple queries on the network
cancer_model.is_active_trail('Pollution', 'Smoker')
cancer_model.is_active_trail('Pollution', 'Smoker', observed=['Cancer'])
cancer_model.get_cpds()
print(cancer_model.get_cpds('Pollution'))
```

```
print(cancer_model.get_cpds('Smoker'))

print(cancer_model.get_cpds('Xray'))
print(cancer_model.get_cpds('Dyspnoea'))
print(cancer_model.get_cpds('Cancer'))
```

7.1.4 Determining the Local independencies

```
cancer_model.local_independencies('Xray')
cancer_model.local_independencies('Pollution')
cancer_model.local_independencies('Smoker')
cancer_model.local_independencies('Dyspnoea')
cancer_model.local_independencies('Cancer')
cancer_model.get_independencies()
```

7.1.5.Inferencing with Bayesian Network

```
# Doing exact inference using Variable Elimination
from pgmpy.inference import VariableElimination
cancer_infer = VariableElimination(cancer_model)

# Computing the probability of bronc given smoke.
q = cancer_infer.query(variables=['Cancer'], evidence={'Smoker': 1})
print(q['Cancer'])
# Computing the probability of bronc given smoke.
q = cancer_infer.query(variables=['Cancer'], evidence={'Smoker': 1})
print(q['Cancer'])
# Computing the probability of bronc given smoke.
q = cancer_infer.query(variables=['Cancer'], evidence={'Smoker': 1,'Pollut
ion': 1})
print(q['Cancer'])
```

7.2 Diagnosis of heart patients using standard Heart Disease Data Set

```
import numpy as np
from urllib.request import urlopen
import urllib
import matplotlib.pyplot as plt # Visuals
import seaborn as sns
import sklearn as skl
import pandas as pd
```

7.2.1 Importing Heart Disease Data Set and Customizing

```
Cleveland_data_URL = 'http://archive.ics.uci.edu/ml/machine-learning-datab
ases/heart-disease/processed.hungarian.data'
```

```python
#Hungarian_data_URL = 'http://archive.ics.uci.edu/ml/machine-learning-data
bases/heart-disease/processed.hungarian.data'
#Switzerland_data_URL = 'http://archive.ics.uci.edu/ml/machine-learning-da
tabases/heart-disease/processed.switzerland.data'
np.set_printoptions(threshold=np.nan) #see a whole array when we output it

names = ['age', 'sex', 'cp', 'trestbps', 'chol', 'fbs', 'restecg', 'thalac
h', 'exang', 'oldpeak', 'slope', 'ca', 'thal', 'heartdisease']
heartDisease = pd.read_csv(urlopen(Cleveland_data_URL), names = names) #ge
ts Cleveland data
#HungarianHeartDisease = pd.read_csv(urlopen(Hungarian_data_URL), names =
names) #gets Hungary data
#SwitzerlandHeartDisease = pd.read_csv(urlopen(Switzerland_data_URL), name
s = names) #gets Switzerland data
#datatemp = [ClevelandHeartDisease, HungarianHeartDisease, SwitzerlandHear
tDisease] #combines all arrays into a list
#heartDisease = pd.concat(datatemp)#combines list into one array
heartDisease.head()
del heartDisease['ca']
del heartDisease['slope']
del heartDisease['thal']
del heartDisease['oldpeak']

heartDisease = heartDisease.replace('?', np.nan)
heartDisease.dtypes
heartDisease.columns
```

7.2.2 Modeling Heart Disease Data

```python
from pgmpy.models import BayesianModel
from pgmpy.estimators import MaximumLikelihoodEstimator, BayesianEstimator

model = BayesianModel([('age', 'trestbps'), ('age', 'fbs'), ('sex', 'trest
bps'), ('sex', 'trestbps'),
                        ('exang', 'trestbps'),('trestbps','heartdisease'),(
'fbs','heartdisease'),
                        ('heartdisease','restecg'),('heartdisease','thalach'
),('heartdisease','chol')])

# Learing CPDs using Maximum Likelihood Estimators
model.fit(heartDisease, estimator=MaximumLikelihoodEstimator)
#for cpd in model.get_cpds():
 #   print("CPD of {variable}:".format(variable=cpd.variable))
  #   print(cpd)
print(model.get_cpds('age'))

print(model.get_cpds('chol'))
print(model.get_cpds('sex'))
model.get_independencies()
```

7.2.3.Inferencing with Bayesian Network

```python
# Doing exact inference using Variable Elimination
from pgmpy.inference import VariableElimination
HeartDisease_infer = VariableElimination(model)


# Computing the probability of bronc given smoke.
q = HeartDisease_infer.query(variables=['heartdisease'], evidence={'age': 28}
)
print(q['heartdisease'])
```

```
╒═══════════════╤════════════════════╕
│ heartdisease  │ phi(heartdisease)  │
╞═══════════════╪════════════════════╡
│ heartdisease_0 │             0.6333 │
├───────────────┼────────────────────┤
│ heartdisease_1 │             0.3667 │
╘═══════════════╧════════════════════╛
```

```python
q = HeartDisease_infer.query(variables=['heartdisease'], evidence={'chol': 10
0})
print(q['heartdisease'])
```

```
╒═══════════════╤════════════════════╕
│ heartdisease  │ phi(heartdisease)  │
╞═══════════════╪════════════════════╡
│ heartdisease_0 │             1.0000 │
├───────────────┼────────────────────┤
│ heartdisease_1 │             0.0000 │
╘═══════════════╧════════════════════╛
```

Program 8 : Apply **EM algorithm** to cluster a set of data stored in a .CSV file. Use the same data set for clustering using **k-Means algorithm**. Compare the results of these two algorithms and comment on the quality of clustering. You can add Java/Python ML library classes/API in the program.

Algorithm :
Expectation Maximization (EM) Algorithm

- When to use:
    - Data is only partially observable
    - Unsupervised clustering (target value unobservable)
    - Supervised learning (some instance attributes unobservable)
- Some uses:
    - Train Bayesian Belief Networks
    - Unsupervised clustering (AUTOCLASS)
    - Learning Hidden Markov Models

Generating Data from Mixture of *k* Gaussians
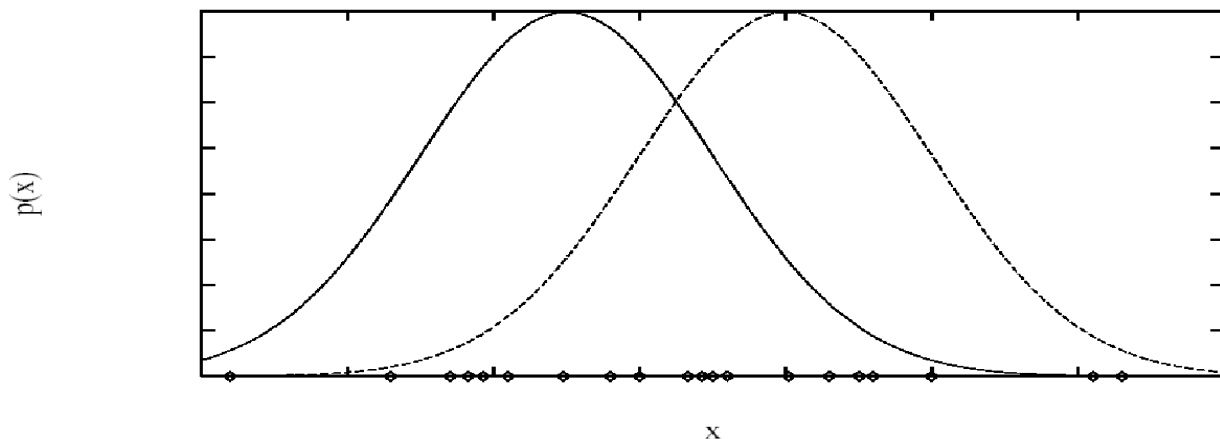
- **Each instance x generated by**

    1. Choosing one of the *k* Gaussians with uniform probability
    2. Generating an instance at random according to that Gaussian

EM for Estimating *k* Means

- Given:
  - Instances from *X* generated by mixture of *k* Gaussian distributions
  - Unknown means $\langle\mu_1,\ldots,\mu_k\rangle$ of the *k* Gaussians
  - Don't know which instance x_i was generated by which Gaussian
- Determine:
  - Maximum likelihood estimates of $\langle\mu_1,\ldots,\mu_k\rangle$
- Think of full description of each instance as
  - $y_i = \langle x_i, z_{i1}, z_{i2}\rangle$ where
    - z_{ij} is 1 if x_i generated by *j*th Gaussian
    - x_i observable
    - z_{ij} unobservable

- **EM Algorithm: Pick random initial $h = \langle\mu_1, \mu_2\rangle$ then iterate**

E step: Calculate the expected value $E[z_{ij}]$ of each
hidden variable z_{ij}, assuming the current
hypothesis
$h = \langle\mu_1, \mu_2\rangle$ holds.

$$
\begin{aligned}
E[z_{ij}] &= \frac{p(x = x_i | \mu = \mu_j)}{\Sigma_{n=1}^{2} \, p(x = x_i | \mu = \mu_n)} \\
&= \frac{e^{-\frac{1}{2\sigma^2}(x_i - \mu_j)^2}}{\Sigma_{n=1}^{2} \, e^{-\frac{1}{2\sigma^2}(x_i - \mu_n)^2}}
\end{aligned}
$$

M step: Calculate a new maximum likelihood hypothesis $h' = \langle\mu'_1, \mu'_2\rangle$, assuming the
value taken on by each hidden variable z_{ij} is its expected value $E[z_{ij}]$ calculated above.
Replace $h = \langle\mu_1, \mu_2\rangle$ by $h' = \langle\mu'_1, \mu'_2\rangle$.

$$
\mu_j \leftarrow \frac{\Sigma_{i=1}^{m} E[z_{ij}] \; x_i}{\Sigma_{i=1}^{m} E[z_{ij}]}
$$

K Means Algorithm

- 1. The sample space is initially partitioned into K clusters and the observations are randomly assigned to the clusters.
- 2. For each sample:
  - Calculate the distance from the observation to the centroid of the cluster.
  - IF the sample is closest to its own cluster THEN leave it ELSE select another cluster.
- 3. Repeat steps 1 and 2 untill no observations are moved from one cluster to another

Distance functions

Euclidean $\sqrt{\sum_{i=1}^{k}(x_i - y_i)^2}$

Manhattan $\sum_{i=1}^{k}|x_i - y_i|$

Minkowski $\left(\sum_{i=1}^{k}(|x_i - y_i|)^q\right)^{1/q}$

Basic Algorithm of K-means

Algorithm 1 Basic K-means Algorithm.

1: Select K points as the initial centroids.
2: **repeat**
3:    Form K clusters by assigning all points to the closest centroid.
4:    Recompute the centroid of each cluster.
5: **until** The centroids don't change

Details of K-means

1. Initial centroids are often chosen randomly.
   - *Clusters produced vary from one run to another*

2. The centroid is (typically) the mean of the points in the cluster.

3. 'Closeness' is measured by **Euclidean distance**, cosine similarity, correlation, etc.

4. K-means will converge for common similarity measures mentioned above.

5. Most of the convergence happens in the first few iterations.
   - *Often the stopping condition is changed to 'Until relatively few points change clusters'*

Euclidean Distance

$$d(i,j) = \sqrt{|x_{i1} - x_{j1}|^2 + |x_{i2} - x_{j2}|^2 + ... + |x_{ip} - x_{jp}|^2}$$

A simple example: Find the distance between two points, the original and the point (3,4)

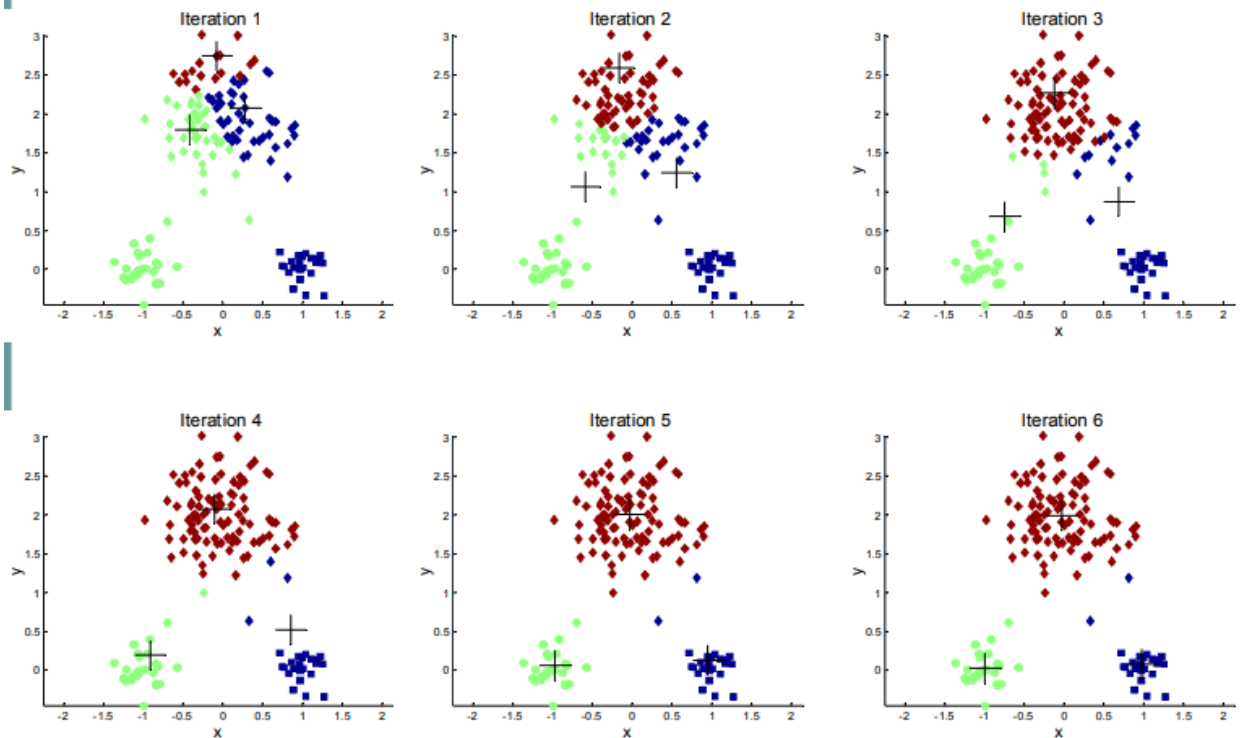$$d_E(O, A) = \sqrt{3^2 + 4^2} = 5$$

Update Centroid

We use the following equation to calculate the n dimensional centroid point amid k n-dimensional points

$$CP(x_1, x_2, ..., x_k) = (\frac{\sum_{i=1}^{k} x1st_i}{k}, \frac{\sum_{i=1}^{k} x2nd_i}{k}, ..., \frac{\sum_{i=1}^{k} xnth_i}{k})$$

Example: Find the centroid of 3 2D points, (2,4), (5,2) and (8,9)

$$CP = (\frac{2+5+8}{3}, \frac{4+2+9}{3}) = (5,5)$$

Examples of K Means

Source Code :

```python
import matplotlib.pyplot as plt
from sklearn import datasets
from sklearn.cluster import KMeans
import sklearn.metrics as sm
import pandas as pd
import numpy as np
%matplotlib inline

# import some data to play with
iris = datasets.load_iris()

#print("\n IRIS DATA :",iris.data);
#print("\n IRIS FEATURES :\n",iris.feature_names)
#print("\n IRIS TARGET :\n",iris.target)
#print("\n IRIS TARGET NAMES:\n",iris.target_names)

# Store the inputs as a Pandas Dataframe and set the column names
X = pd.DataFrame(iris.data)

#print(X)
X.columns = ['Sepal_Length','Sepal_Width','Petal_Length','Petal_Width']
```

```python
#print(X.columns)
#print("X:",x)
#print("Y:",y)
y = pd.DataFrame(iris.target)
y.columns = ['Targets']

# Set the size of the plot
plt.figure(figsize=(14,7))

# Create a colormap
colormap = np.array(['red', 'lime', 'black'])

# Plot Sepal
plt.subplot(1, 2, 1)
plt.scatter(X.Sepal_Length,X.Sepal_Width, c=colormap[y.Targets], s=40)
plt.title('Sepal')

plt.subplot(1, 2, 2)
plt.scatter(X.Petal_Length,X.Petal_Width, c=colormap[y.Targets], s=40)
plt.title('Petal')
```

Text(0.5,1,'Petal')

Build the K Means Model

```python
# K Means Cluster
model = KMeans(n_clusters=3)
model.fit(X)
# This is what KMeans thought
model.labels_
```

array([0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
**   0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0**
,

```
      0, 0, 0, 0, 1, 1, 2, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1
,
      1, 1, 1, 1, 1, 1, 1, 1, 2, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1
,
      1, 1, 1, 1, 1, 1, 1, 1, 2, 1, 2, 2, 2, 2, 1, 2, 2, 2, 2, 2, 2, 1, 1
,
      2, 2, 2, 2, 1, 2, 1, 2, 1, 2, 2, 1, 1, 2, 2, 2, 2, 2, 1, 2, 2, 2, 2
,
      1, 2, 2, 2, 1, 2, 2, 2, 1, 2, 2, 1])
```

Visualise the classifier results

```
# View the results
# Set the size of the plot
plt.figure(figsize=(14,7))

# Create a colormap
colormap = np.array(['red', 'lime', 'black'])

# Plot the Original Classifications
plt.subplot(1, 2, 1)
plt.scatter(X.Petal_Length, X.Petal_Width, c=colormap[y.Targets], s=40)
plt.title('Real Classification')

# Plot the Models Classifications
plt.subplot(1, 2, 2)
plt.scatter(X.Petal_Length, X.Petal_Width, c=colormap[model.labels_], s=40
)
plt.title('K Mean Classification')
```

```
Text(0.5,1,'K Mean Classification')
```


The Fix

```
# The fix, we convert all the 1s to 0s and 0s to 1s.
predY = np.choose(model.labels_, [0, 1, 2]).astype(np.int64)
print (predY)
```

```
[0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
 0 0 0 0 0 0 0 0 0 0 0 0 0 0 1 1 2 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
 1 1 1 2 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 2 1 2 2 2 2 1 2 2 2 2
 2 2 1 1 2 2 2 2 1 2 1 2 1 2 2 1 1 2 2 2 2 2 1 2 2 2 2 1 2 2 2 1 2 2 2 1 2 2 2 1 2
 2 1]
```

Re-plot

```python
# View the results
# Set the size of the plot
plt.figure(figsize=(14,7))

# Create a colormap
colormap = np.array(['red', 'lime', 'black'])

# Plot Orginal
plt.subplot(1, 2, 1)
plt.scatter(X.Petal_Length, X.Petal_Width, c=colormap[y.Targets], s=40)
plt.title('Real Classification')

# Plot Predicted with corrected values
plt.subplot(1, 2, 2)
plt.scatter(X.Petal_Length,X.Petal_Width, c=colormap[predY], s=40)
plt.title('K Mean Classification')
```

```
Text(0.5,1,'K Mean Classification')
```


Performance Measures

Accuracy

```
sm.accuracy_score(y, model.labels_)
```

```
0.89333333333333331
```

Confusion Matrix

```
# Confusion Matrix
sm.confusion_matrix(y, model.labels_)
array([[50,  0,  0],
       [ 0, 48,  2],
       [ 0, 14, 36]], dtype=int64)
```

GMM

```
from sklearn import preprocessing

scaler = preprocessing.StandardScaler()

scaler.fit(X)
xsa = scaler.transform(X)
xs = pd.DataFrame(xsa, columns = X.columns)
xs.sample(5)
```

	Sepal_Length	Sepal_Width	Petal_Length	Petal_Width
132	0.674501	-0.587764	1.047087	1.316483
110	0.795669	0.337848	0.762759	1.053537
93	-1.021849	-1.744778	-0.260824	-0.261193
24	-1.264185	0.800654	-1.056944	-1.312977
111	0.674501	-0.819166	0.876490	0.922064

```
from sklearn.mixture import GaussianMixture
gmm = GaussianMixture(n_components=3)
gmm.fit(xs)
```

```
GaussianMixture(covariance_type='full', init_params='kmeans', max_iter=100
,
        means_init=None, n_components=3, n_init=1, precisions_init=None,
        random_state=None, reg_covar=1e-06, tol=0.001, verbose=0,
        verbose_interval=10, warm_start=False, weights_init=None)
y_cluster_gmm = gmm.predict(xs)
y_cluster_gmm
array([0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0
,
        0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0
,
        0, 0, 0, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 2
,
        1, 2, 1, 2, 1, 1, 1, 1, 2, 1, 1, 1, 1, 1, 2, 1, 1, 1, 1, 1, 1, 1, 1
,
        1, 1, 1, 1, 1, 1, 1, 1, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2
,
```

```
      2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2
,
      2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2], dtype=int32)
plt.subplot(1, 2, 1)
plt.scatter(X.Petal_Length, X.Petal_Width, c=colormap[y_cluster_gmm], s=40
)
plt.title('GMM Classification')
```

ext(0.5,1,'GMM Classification')


```
sm.accuracy_score(y, y_cluster_gmm)
```

0.96666666666666667

```
# Confusion Matrix
sm.confusion_matrix(y, y_cluster_gmm)
array([[50,  0,  0],
       [ 0, 45,  5],
       [ 0,  0, 50]], dtype=int64)
```

```
# so the GMM clustering matched the true labels more closely than the Kmea
ns,
# as expected from the plots.
```

Program9 : Write a program to implement k-Nearest Neighbour algorithm to classify the iris data set. Print both correct and wrong predictions. Java/Python ML library classes can be used for this problem.

Algorithm :

K-Nearest-Neighbor Algorithm

- **Principle: points (documents) that are close in the space belong to the same class**
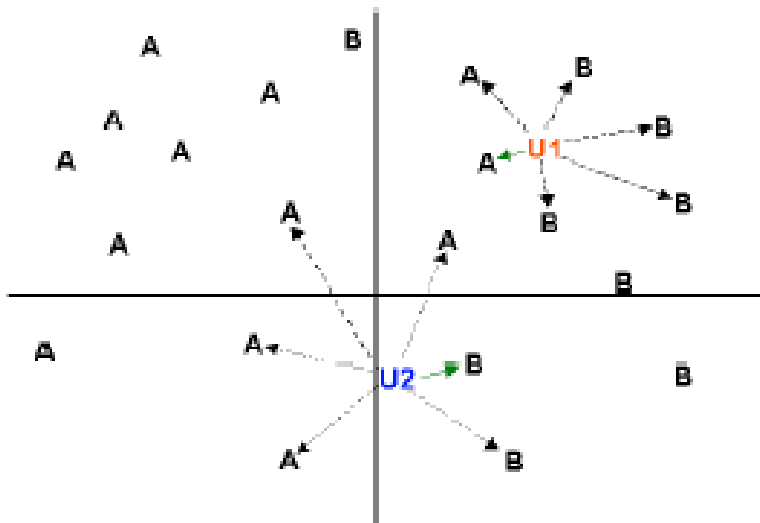
Definition of Nearest Neighbor
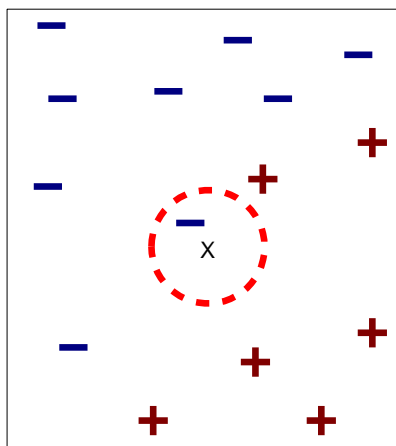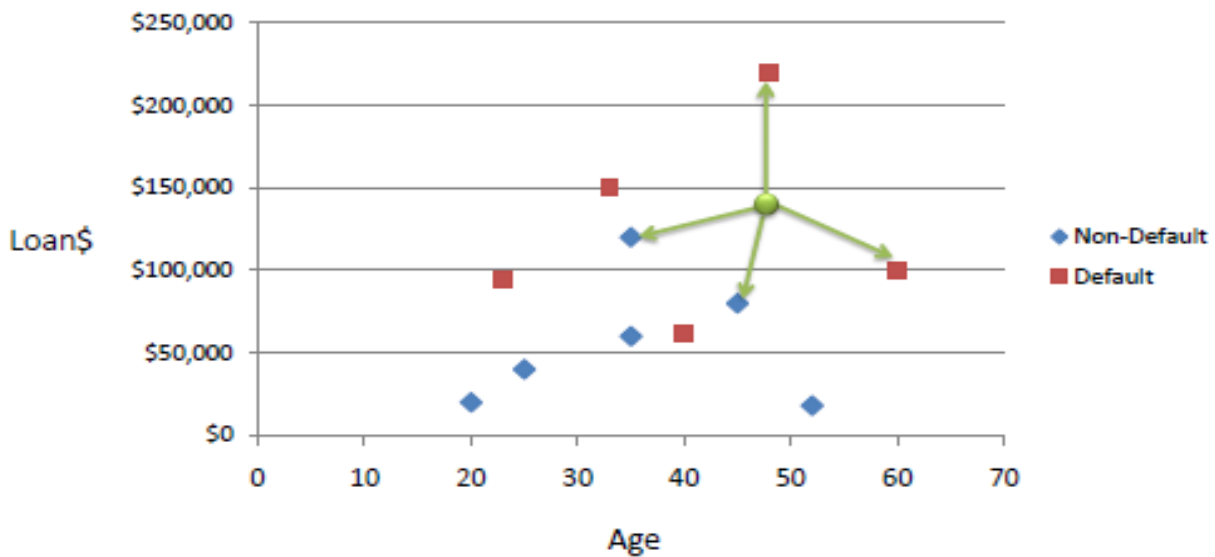

(a) 1-nearest neighbor   (b) 2-nearest neighbor   (c) 3-nearest neighbor
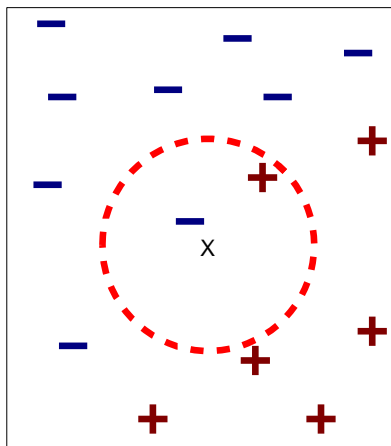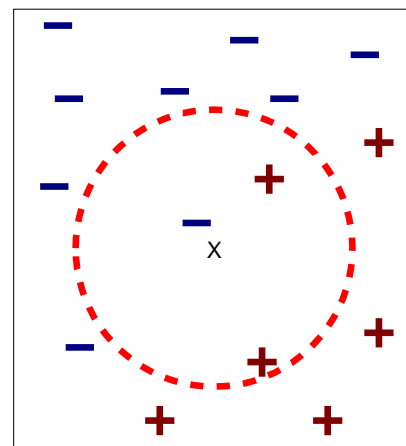
Distance Metrics

Minkowsky:

$$D(\boldsymbol{x},\boldsymbol{y}) = \left(\sum_{i=1}^{m} |x_i - y_i|^r \right)^{1/r}$$

Euclidean:

$$D(\boldsymbol{x},\boldsymbol{y}) = \sqrt{\sum_{i=1}^{m} (x_i - y_i)^2}$$

Manhattan / city-block:

$$D(\boldsymbol{x},\boldsymbol{y}) = \sum_{i=1}^{m} |x_i - y_i|$$

Camberra:

$$D(\boldsymbol{x},\boldsymbol{y}) = \sum_{i=1}^{m} \frac{|x_i - y_i|}{|x_i + y_i|}$$

Chebychev:

$$D(\boldsymbol{x},\boldsymbol{y}) = \max_{i=1}^{m} |x_i - y_i|$$

Quadratic:

$$D(\boldsymbol{x},\boldsymbol{y}) = (\boldsymbol{x}-\boldsymbol{y})^T Q (\boldsymbol{x}-\boldsymbol{y}) = \sum_{j=1}^{m} \left(\sum_{i=1}^{m} (x_i - y_i) q_{ji} \right) (x_j - y_j)$$

Q is a problem-specific positive definite $m \times m$ weight matrix

Mahalanobis:

$$D(\boldsymbol{x},\boldsymbol{y}) = [\det V]^{1/m} (\boldsymbol{x}-\boldsymbol{y})^T V^{-1} (\boldsymbol{x}-\boldsymbol{y})$$

V is the covariance matrix of $A_1..A_m$, and A_j is the vector of values for attribute j occuring in the training set instances $1..n$.

Correlation:

$$D(\boldsymbol{x},\boldsymbol{y}) = \frac{\sum_{i=1}^{m} (x_i - \overline{x_i})(y_i - \overline{y_i})}{\sqrt{\sum_{i=1}^{m} (x_i - \overline{x_i})^2 \sum_{i=1}^{m} (y_i - \overline{y_i})^2}}$$

$\overline{x_i} = \overline{y_i}$ and is the average value for attribute i occuring in the training set.

Chi-square:

$$D(\boldsymbol{x},\boldsymbol{y}) = \sum_{i=1}^{m} \frac{1}{sum_i} \left(\frac{x_i}{size_x} - \frac{y_i}{size_y} \right)^2$$

sum_i is the sum of all values for attribute i occuring in the training set, and $size_x$ is the sum of all values in the vector $\boldsymbol{x}$.

Kendall's Rank Correlation:

$$D(\boldsymbol{x},\boldsymbol{y}) = 1 - \frac{2}{n(n-1)} \sum_{i=1}^{m} \sum_{j=1}^{i-1} \text{sign}(x_i - x_j)\text{sign}(y_i - y_j)$$

$\text{sign}(x) = -1, 0$ or 1 if $x < 0$, $x = 0$, or $x > 0$, respectively.

Figure 1. Equations of selected distance functions.
($\boldsymbol{x}$ and $\boldsymbol{y}$ are vectors of m attribute values).

Example: Consider the following data concerning credit default. Age and Loan are two numerical variables (predictors) and Default is the target.

We can now use the training set to classify an unknown case (Age=48 and Loan=$142,000) using Euclidean distance. If K=1 then the nearest neighbor is the last case in the training set with Default=Y.
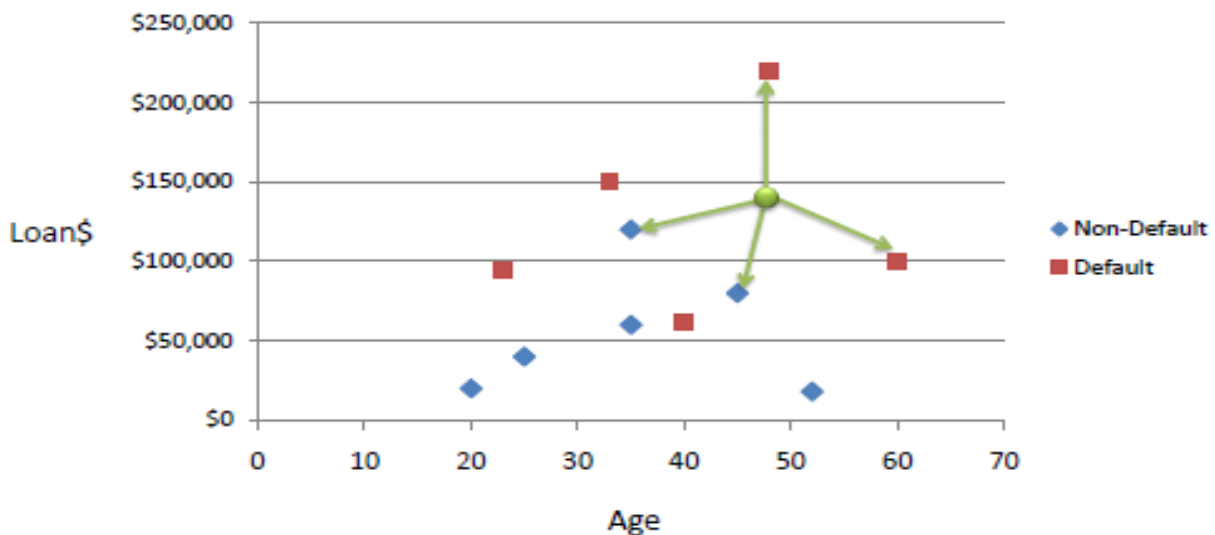
$$D = Sqrt[(48-33)^2 + (142000-150000)^2] = 8000.01 \ >> \ Default=Y$$

Age	Loan	Default	Distance	
25	$40,000	N	102000	
35	$60,000	N	82000	
45	$80,000	N	62000	
20	$20,000	N	122000	
35	$120,000	N	22000	2
52	$18,000	N	124000	
23	$95,000	Y	47000	
40	$62,000	Y	80000	
60	$100,000	Y	42000	3
48	$220,000	Y	78000	
33	$150,000	Y	8000	1
48	$142,000	?		

Euclidean Distance

$$D = \sqrt{(x_1 - y_1)^2 + (x_2 - y_2)^2}$$

With K=3, there are two Default=Y and one Default=N out of three closest neighbors. The prediction for the unknown case is again Default=Y.

Source Code :

```python
# Python program to demonstrate
# KNN classification algorithm
# on IRIS dataset

from sklearn.datasets import load_iris
from sklearn.neighbors import KNeighborsClassifier
import numpy as np
from sklearn.model_selection import train_test_split
iris_dataset=load_iris()

print("\n IRIS FEATURES \ TARGET NAMES: \n ", iris_dataset.target_names)
for i in range(len(iris_dataset.target_names)):
    print("\n[{0}]:[{1}]".format(i,iris_dataset.target_names[i]))
```

```python
print("\n IRIS DATA :\n",iris_dataset["data"])

X_train, X_test, y_train, y_test = train_test_split(iris_dataset["data"],
iris_dataset["target"], random_state=0)

print("\n Target :\n",iris_dataset["target"])
print("\n X TRAIN \n", X_train)
print("\n X TEST \n", X_test)
print("\n Y TRAIN \n", y_train)
print("\n Y TEST \n", y_test)
kn = KNeighborsClassifier(n_neighbors=1)
kn.fit(X_train, y_train)

x_new = np.array([[5, 2.9, 1, 0.2]])
print("\n XNEW \n",x_new)

prediction = kn.predict(x_new)

print("\n Predicted target value: {}\n".format(prediction))
print("\n Predicted feature name: {}\n".format
    (iris_dataset["target_names"][prediction]))

i=1
x= X_test[i]
x_new = np.array([x])
print("\n XNEW \n",x_new)

for i in range(len(X_test)):
    x = X_test[i]
    x_new = np.array([x])
    prediction = kn.predict(x_new)
    print("\n Actual : {0} {1}, Predicted :{2}{3}".format(y_test[i],iris_d
ataset["target_names"][y_test[i]],prediction,iris_dataset["target_names"][
prediction]))

print("\n TEST SCORE[ACCURACY]: {:.2f}\n".format(kn.score(X_test, y_test))
)
```

Output :

```
Actual : 2 virginica, Predicted :[2]['virginica']
Actual : 1 versicolor, Predicted :[1]['versicolor']
Actual : 0 setosa, Predicted :[0]['setosa']
Actual : 2 virginica, Predicted :[2]['virginica']
Actual : 0 setosa, Predicted :[0]['setosa']
--------
Actual : 1 versicolor, Predicted :[2]['virginica']

TEST SCORE[ACCURACY]: 0.97
```

Program10 : Implement the non-parametric Locally Weighted Regression algorithm in order to fit data points. Select appropriate data set for your experiment and draw graphs.
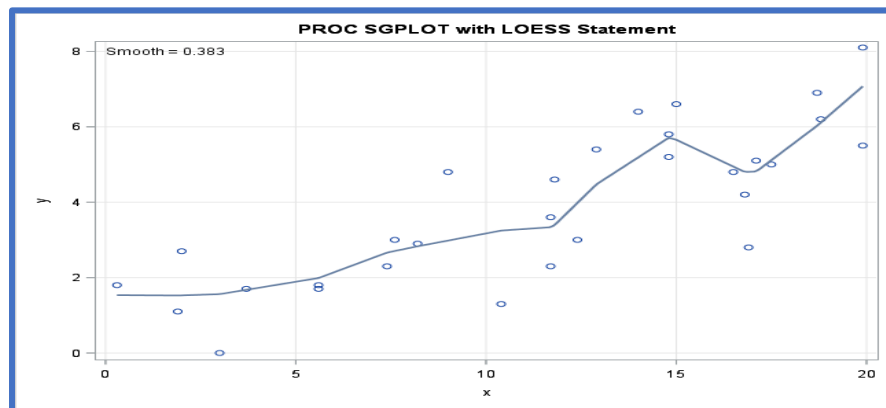
Algorithm :

Regression:

- Regression is a technique from statistics that is used to predict values of a desired target quantity when the target quantity is continuous .
- In regression, we seek to identify (or estimate) a continuous variable y associated with a given input vector x.
  - y is called the dependent variable.
  - x is called the independent variable.
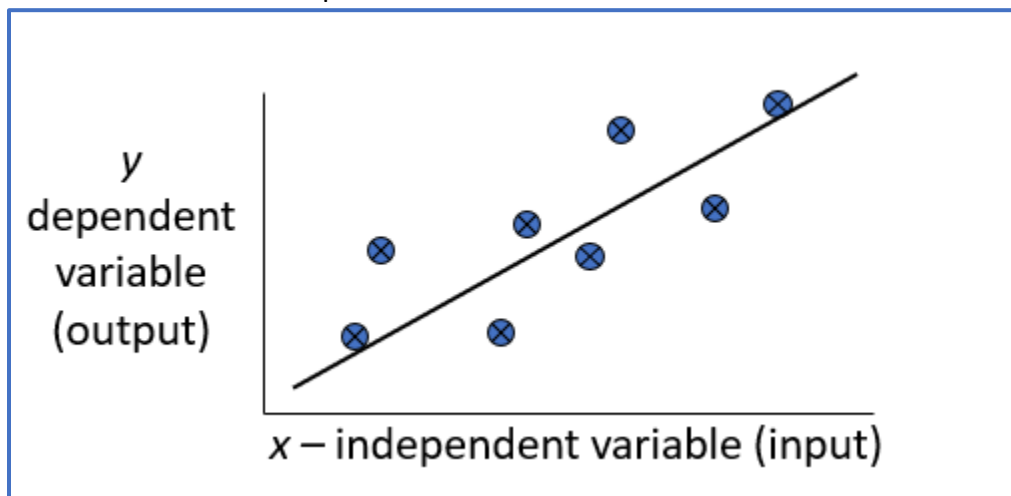
Loess/Lowess Regression: Loess regression is a nonparametric technique that uses *local weighted* regression to fit a smooth curve through points in a scatter plot.

Lowess Algorithm: [Locally weighted regression](#) is a very powerful non-parametric model used in statistical learning .Given a *dataset* X, y, we attempt to find a *model* parameter β(x) that minimizes *residual sum of weighted squared errors*. The weights are given by a *kernel function(k or w)* which can be chosen arbitrarily .

Algorithm

1. **Read the Given data Sample to X and the curve (linear or non linear) to Y**
2. **Set the value for Smoothening parameter or Free parameter say τ**
3. **Set the bias /Point of interest set X0 which is a subset of X**
4. **Determine the weight matrix using :**

$$w(x, x_o) = e^{-\frac{(x-x_o)^2}{2\tau^2}}$$

5. **Determine the value of model term parameter β using :**

$$\hat{\beta}(x_o) = (X^T W X)^{-1} X^T W y$$

6. **Prediction = x0*β**

Source Code :

```
import numpy as np
from bokeh.plotting import figure, show, output_notebook
from bokeh.layouts import gridplot
from bokeh.io import push_notebook

output_notebook()
```

BokehJS 0.12.10 successfully loaded.

```
import numpy as np
```

```python
def local_regression(x0, X, Y, tau):
    # add bias term
    x0 = np.r_[1, x0] # Add one to avoid the loss in information
    X = np.c_[np.ones(len(X)), X]

    # fit model: normal equations with kernel
    xw = X.T * radial_kernel(x0, X, tau)    # XTranspose * W

    beta = np.linalg.pinv(xw @ X) @ xw @ Y    # @ Matrix Multiplication or
Dot Product

    # predict value
    return x0 @ beta    # @ Matrix Multiplication or Dot Product for predi
ction

def radial_kernel(x0, X, tau):
    return np.exp(np.sum((X - x0) ** 2, axis=1) / (-2 * tau * tau))
# Weight or Radial Kernal Bias Function
```

```python
n = 1000
# generate dataset
X = np.linspace(-3, 3, num=n)
print("The Data Set ( 10 Samples) X :\n",X[1:10])
Y = np.log(np.abs(X ** 2 - 1) + .5)
print("The Fitting Curve Data Set (10 Samples) Y  :\n",Y[1:10])
# jitter X
X += np.random.normal(scale=.1, size=n)
print("Normalised (10 Samples) X :\n",X[1:10])
```

```
The Data Set ( 10 Samples) X :
 [-2.99399399 -2.98798799 -2.98198198 -2.97597598 -2.96996997 -2.96396396
 -2.95795796 -2.95195195 -2.94594595]
The Fitting Curve Data Set (10 Samples) Y  :
 [ 2.13582188  2.13156806  2.12730467  2.12303166  2.11874898  2.11445659
   2.11015444  2.10584249  2.10152068]
Normalised (10 Samples) X :
 [-3.17013248 -2.87908581 -3.37488159 -2.90743352 -2.93640374 -2.97978828
 -3.0549104  -3.0735006  -2.88552749]
```
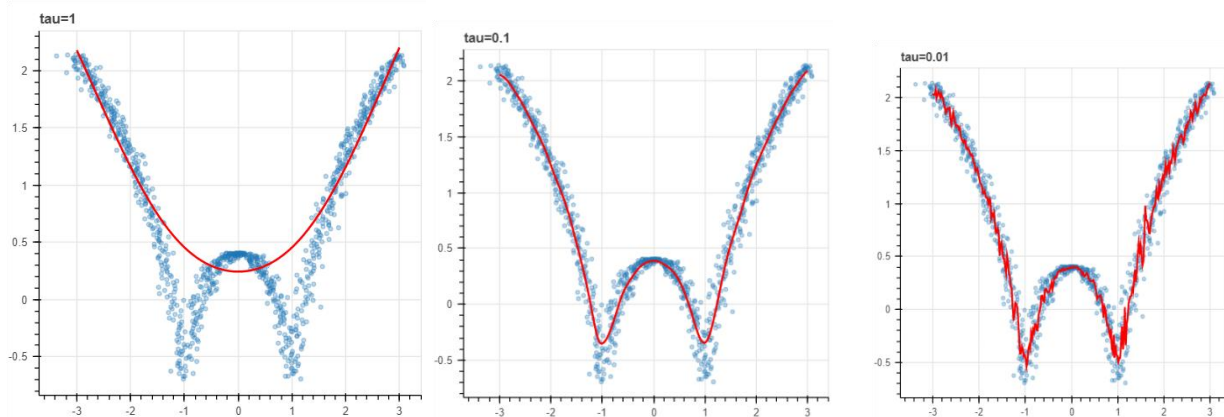
```python
domain = np.linspace(-3, 3, num=300)
print(" Xo Domain Space(10 Samples)  :\n",domain[1:10])

def plot_lwr(tau):
    # prediction through regression
    prediction = [local_regression(x0, X, Y, tau) for x0 in domain]
    plot = figure(plot_width=400, plot_height=400)
    plot.title.text='tau=%g' % tau
    plot.scatter(X, Y, alpha=.3)
    plot.line(domain, prediction, line_width=2, color='red')
    return plot
```

```
Xo Domain Space(10 Samples)  :
 [-2.97993311 -2.95986622 -2.93979933 -2.91973244 -2.89966555 -2.87959866
 -2.85953177 -2.83946488 -2.81939799]
```
```
# Plotting the curves with different tau
show(gridplot([
    [plot_lwr(10.), plot_lwr(1.)],
    [plot_lwr(0.1), plot_lwr(0.01)]
]))
```

Output :

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